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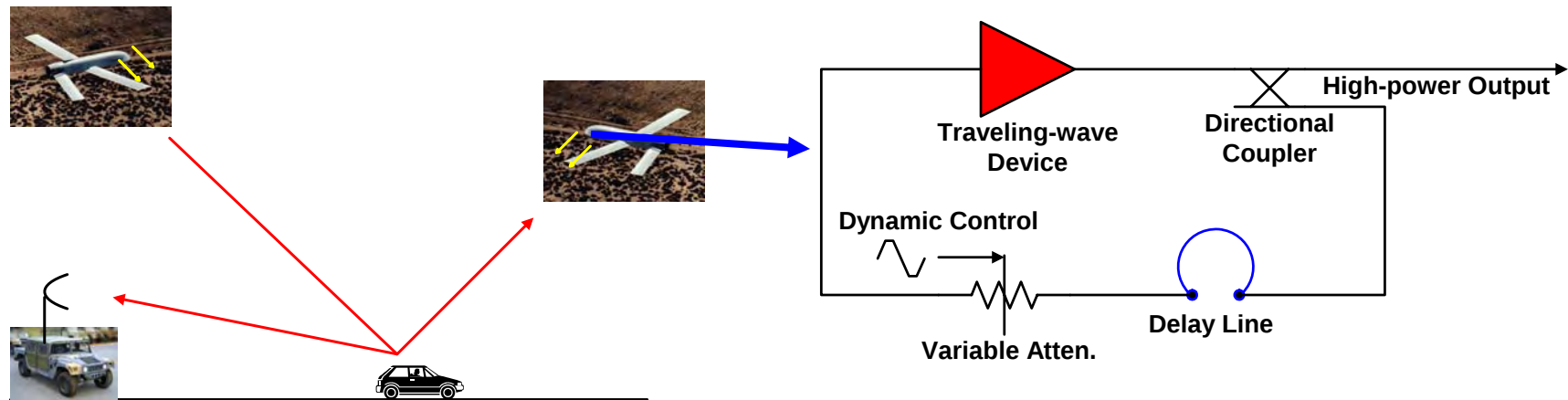
IREAP

Chaotic microwave systems based on traveling-wave tube (TWT) amplifiers

*John Rodgers, Mike Holloway, Kristy Gaff, Michelle Adan
Institute for Research in Electronics and Applied Physics
University of Maryland
College Park, MD 20742*

rodgers@umd.edu

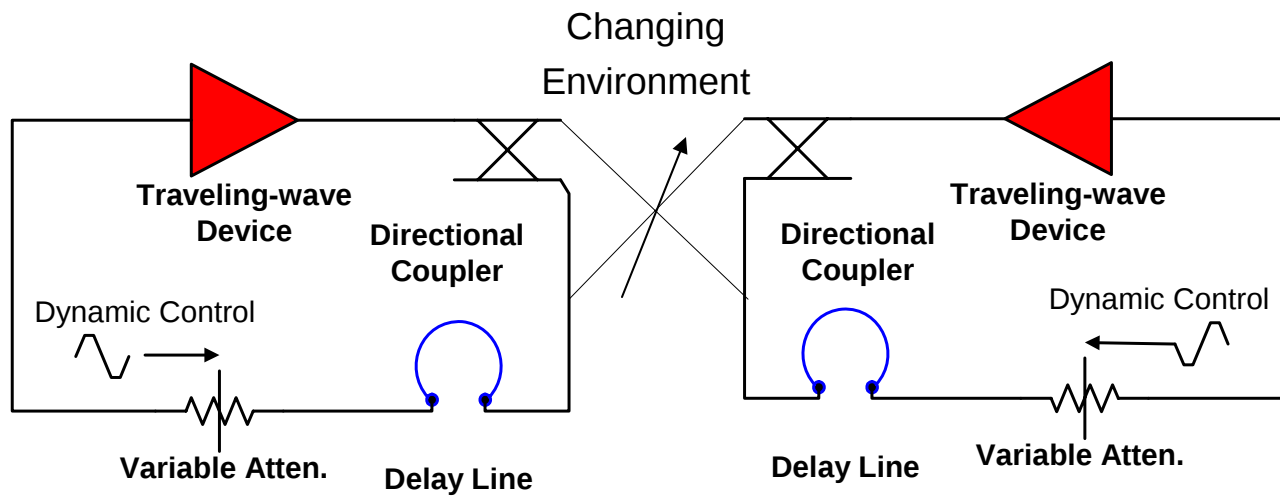
Concept: Networks of coupled chaotic time-delayed oscillators (TDO)



- The radiation scattered off objects will couple in varying strengths to the various nodes of the network and modulate its dynamics.

Basic Research Questions

- How robust would synchronization in the network be in the presence of:
 - Noise
 - Mismatch in the dynamical parameters of the nodes
 - Interference or jamming
 - Complexity of the environment

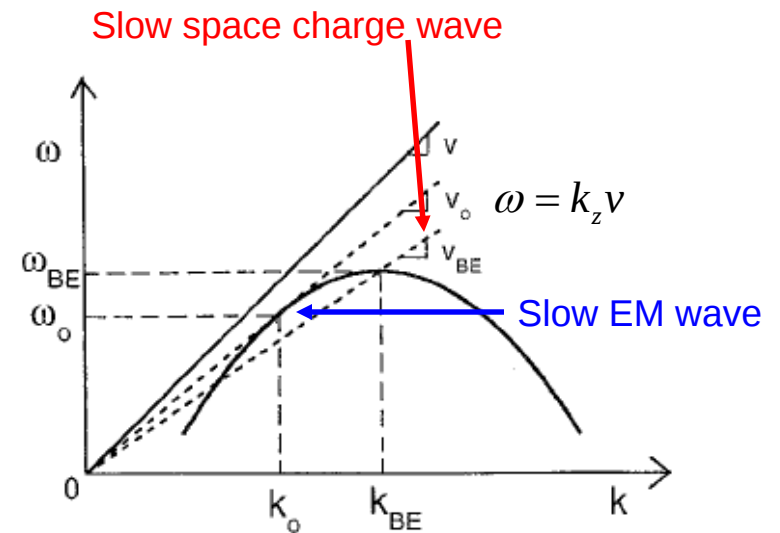
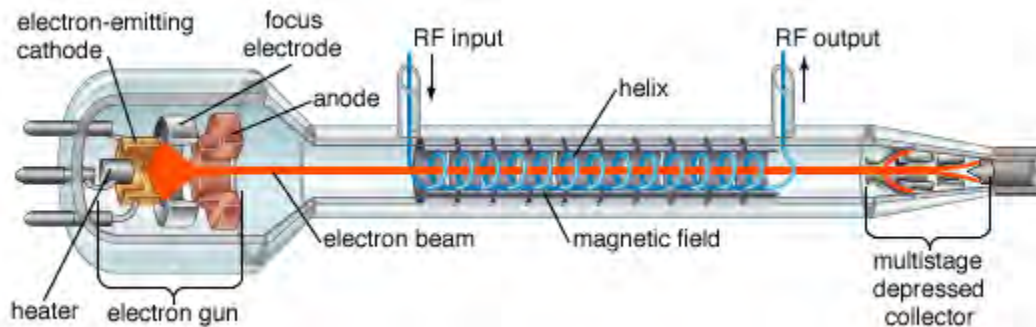




Outline

- Basic characteristics of the traveling-wave tube (TWT)
- TWT nonlinearity
- Saturation models
- Results of previous simulations
- Results of experiments on TWT's with time-delayed feedback
- Digital control of the time-delayed system
- Future research

TWT Basics



TWT Dispersion Diagram

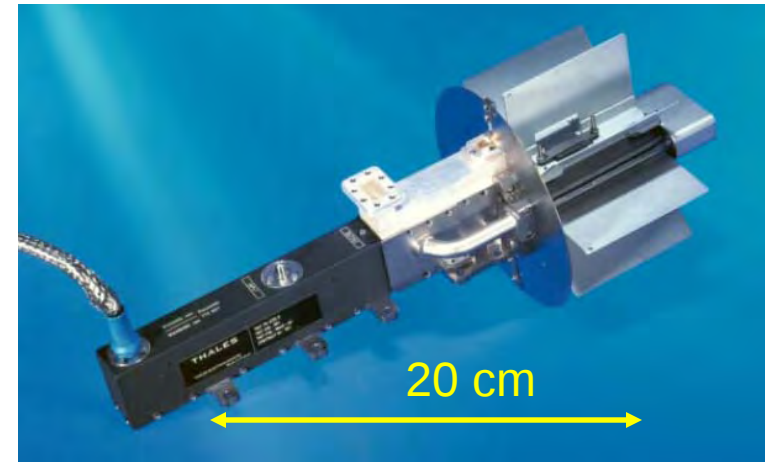
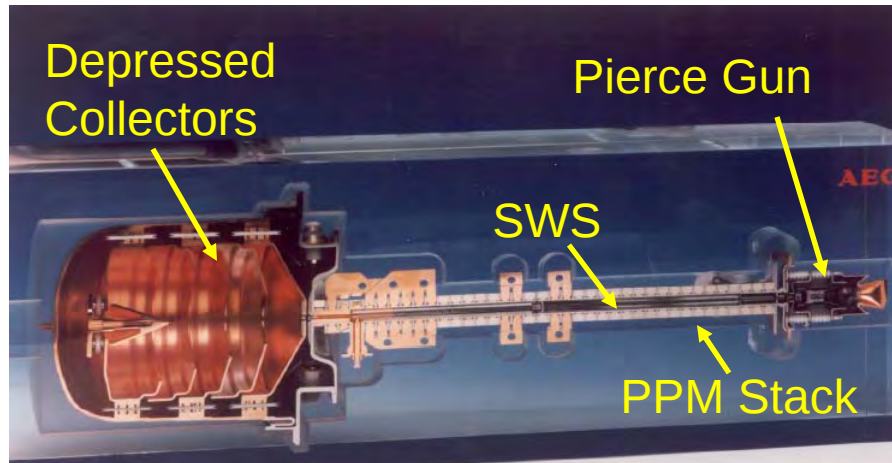
- Properties:

High gain, wideband, good linearity and efficiency

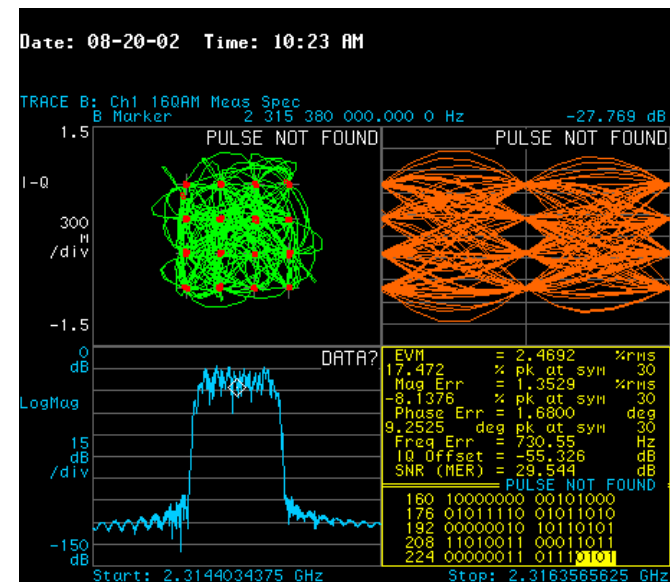
- Applications:

Space communications, secure LOS, cell phones, radar, EW

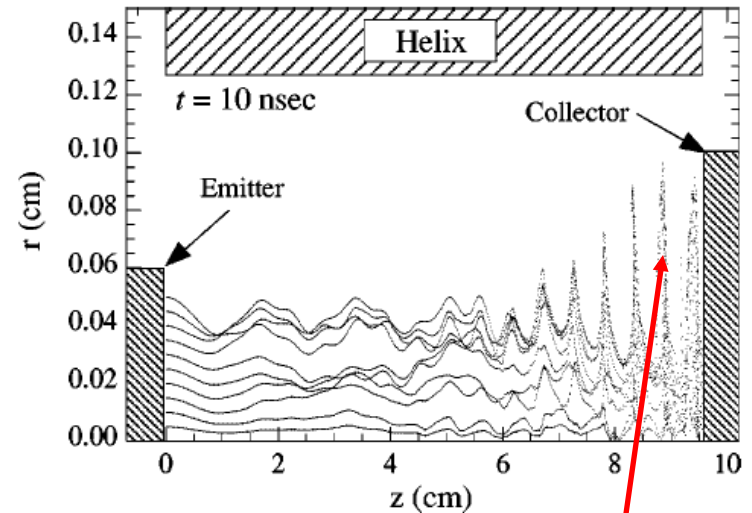
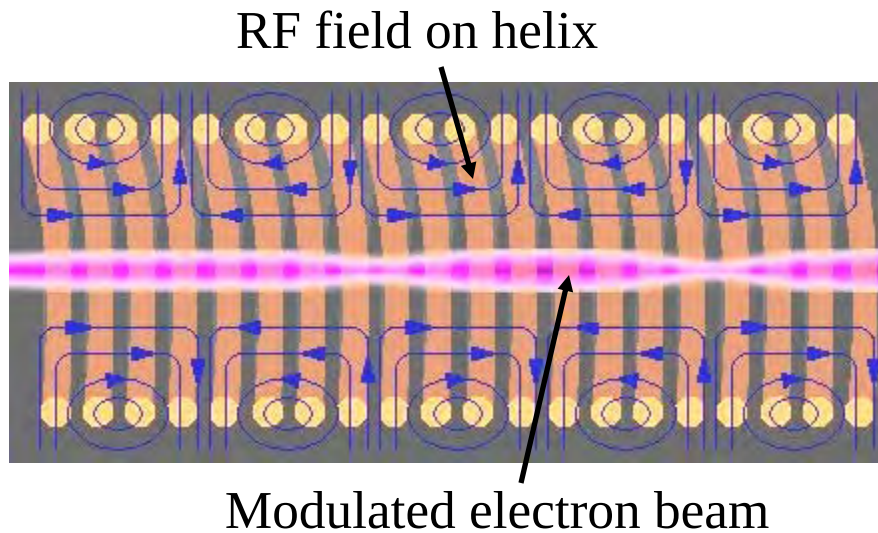
Typical characteristics of the TWTA



- High gain 40-60 dB
- Wideband >2 octaves
- Compact m~ kg, L < 12 cm
- Efficient >80% (Dep. Coll.)
- High Frequency >50 GHz
- Modest Voltage ~few kV



Nonlinearity in TWT's (1-D Model)



Equation of Motion

Continuity

Gauss's Law

Wave Equation

$$\frac{\partial v}{\partial t} = -v \frac{\partial v}{\partial z} - \frac{e}{m} \frac{\partial (V_w + V_{sc})}{\partial z}$$

$$\frac{\partial \rho}{\partial t} = -\frac{\partial (\rho v)}{\partial z}$$

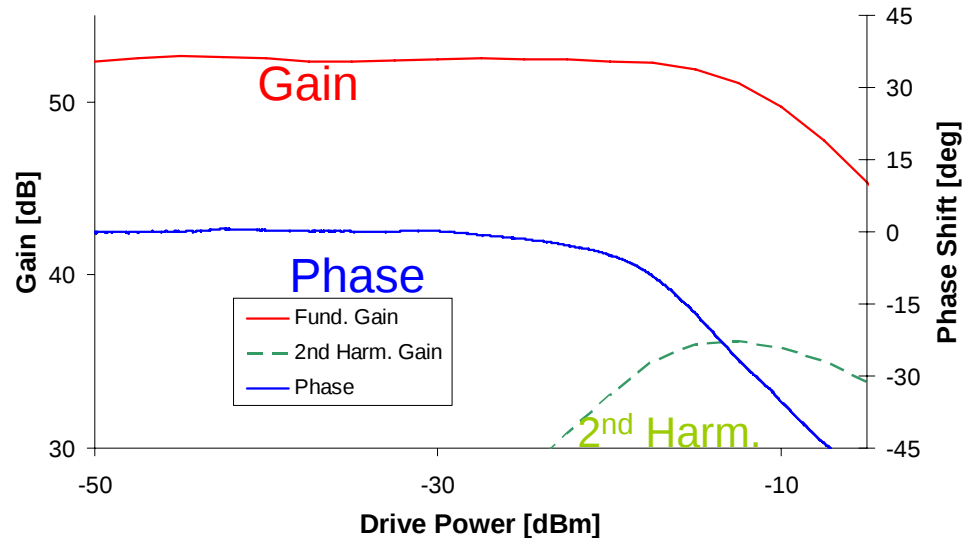
$$\frac{\partial^2 V_{sc}}{\partial z^2} = -\frac{\rho}{\epsilon_0}$$

$$\frac{\partial^2 V_w}{\partial t^2} - c^2 \frac{\partial^2 V_w}{\partial z^2} = c Z_0 A \frac{\partial^2 \rho}{\partial t^2}$$

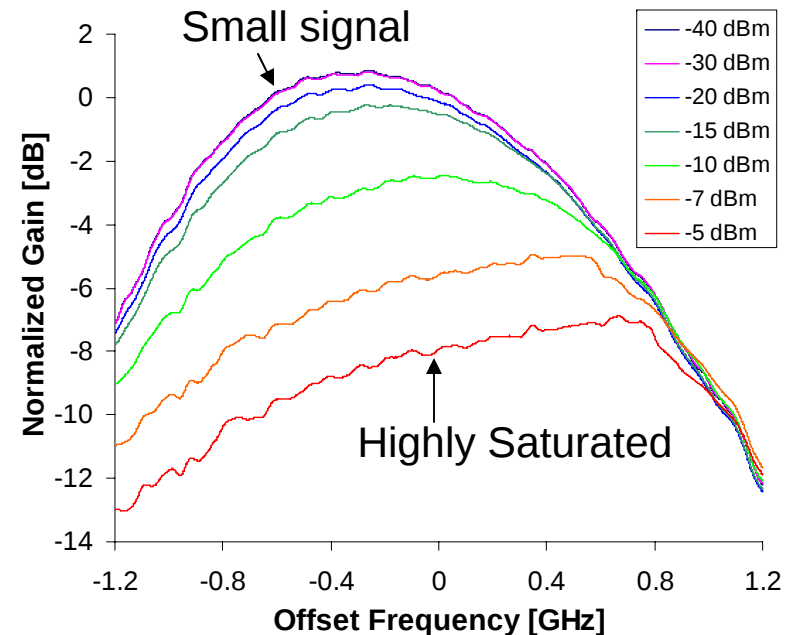
Over-modulation of the beam increases space-charge forces which saturate the amplifier.

TWT Gain Saturation

Gain and Output Phase vs. Input Power



Gain-Bandwidth



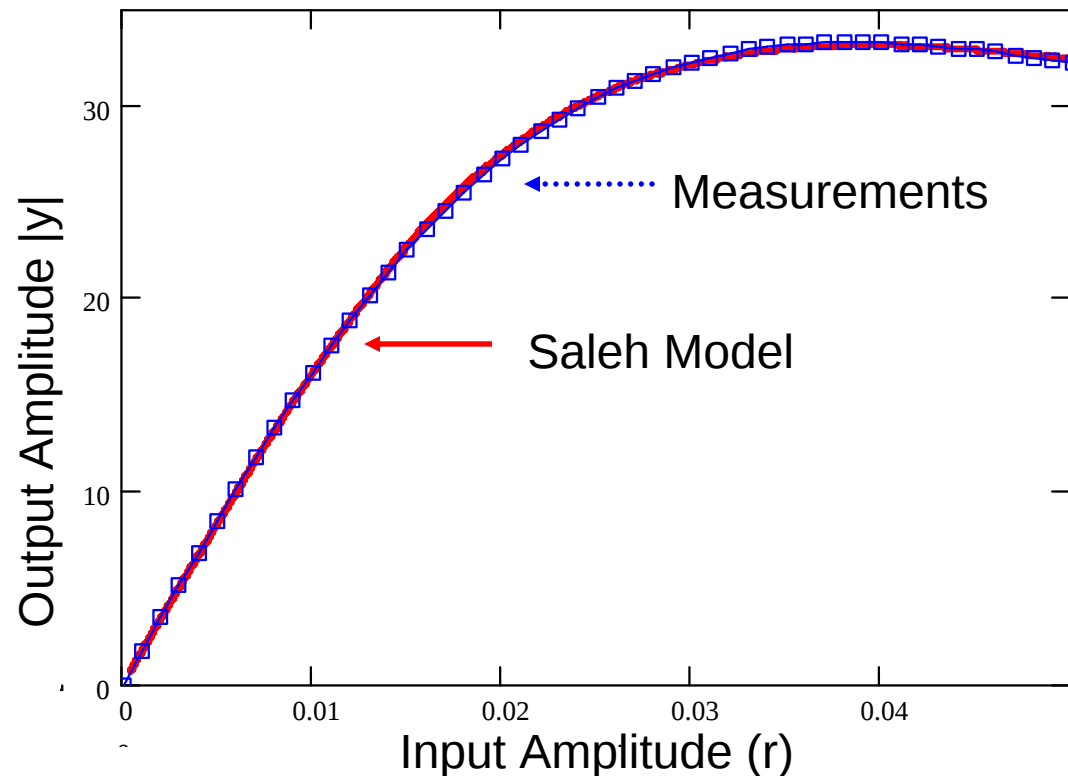
In some TWT's, saturation is well described as a quadratic function of the input amplitude and the small-signal bandwidth as a first-order band pass filter (BPF).

Comparison of measured TWT drive curve with best fit to Saleh¹ model

$$y = A(r)e^{-j\Phi(r)}$$

$$A(r) = \frac{\alpha_a r}{1 + \beta_a r^2}$$

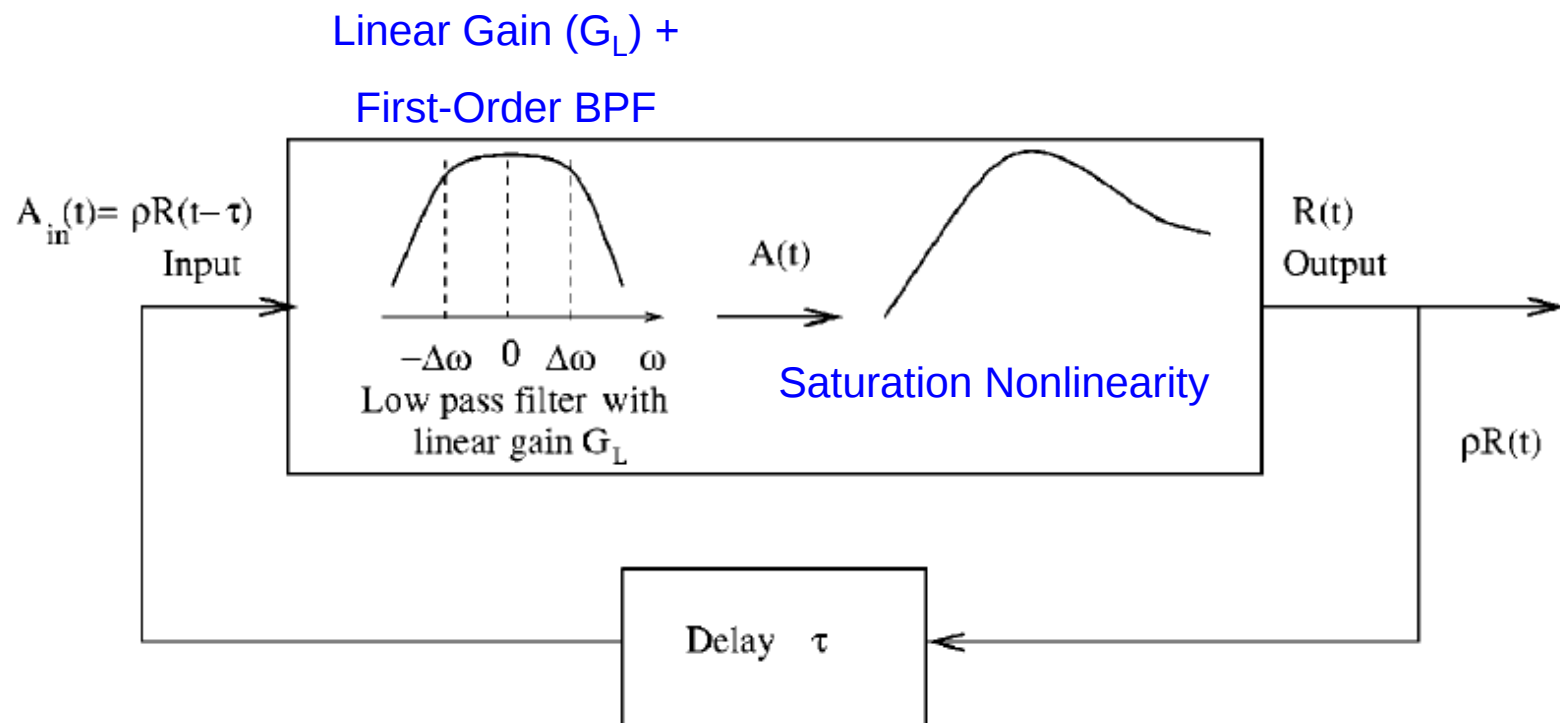
$$\Phi(r) = \frac{\alpha_\phi r^2}{(1 + \beta_\phi r^2)^2}$$



1. A. M. Saleh, *IEEE Trans. Comm.*, Vol. 29, No. 11, (1981), pp. 1715-1720.

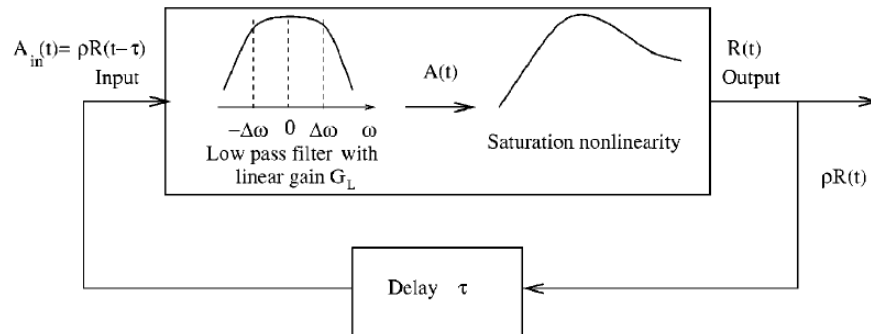
Model of a Time-delayed Feedback Oscillator Using Linear and Nonlinear Blocks to Describe the TWT

(see poster presented by Wai-Shing Lee)



2. V. Dronov, M. Hendry, T. M. Antonsen, Jr., and E. Ott, *Chaos*, Vol. 14, No. 1, pp. 30-35, 2004.

Nonlinear Dynamics



Loop Gain :

$$k = \rho G_L$$

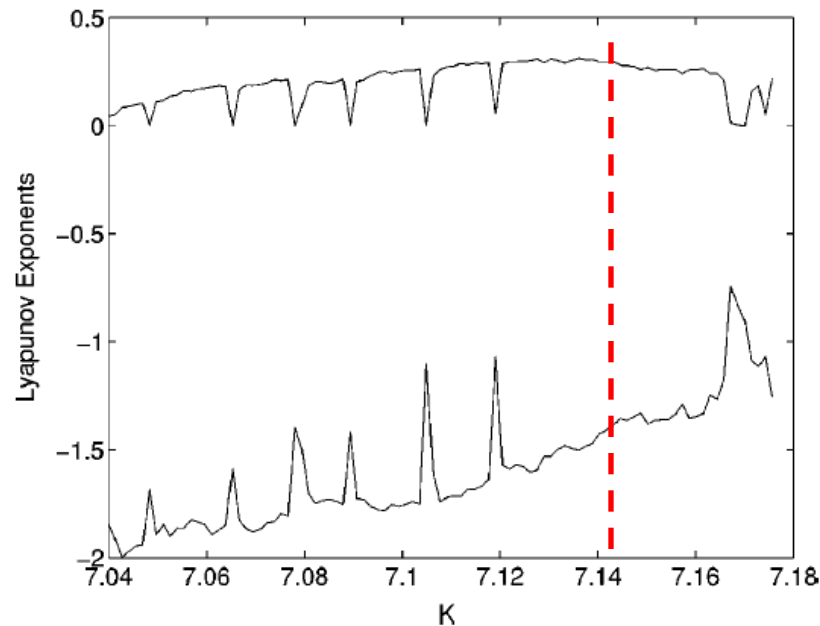
Output :

$$R(t) = A(t) \frac{e^{i\eta|A(t)|^2}}{1 + |A(t)|^2}$$

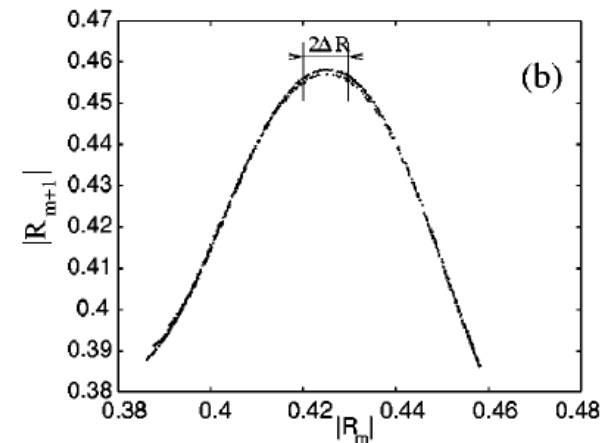
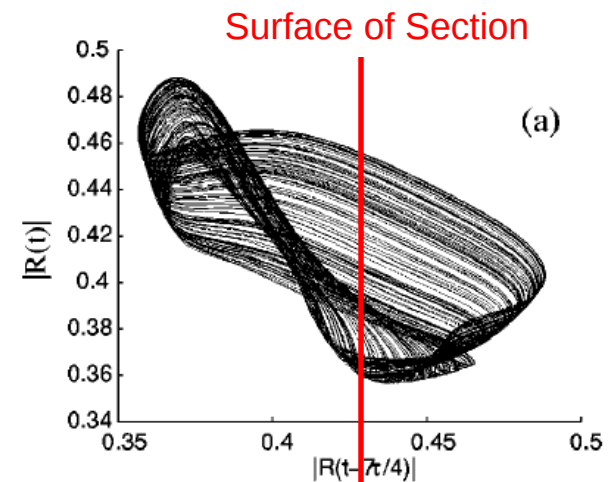
Dimensionless Time : $t \rightarrow t\Delta\omega, \tau \rightarrow \tau\Delta\omega$

$$DDE : \frac{dA(t)}{dt} + A(t) = kA(t - \tau) \frac{e^{i\eta|A(t-\tau)|^2}}{1 + |A(t - \tau)|^2} \rightarrow \text{Quadratic Saturation Model}$$

Numerical Results Using Quadratic Saturation Model



System Parameters: $k = 7.142$
 $\tau = 0.530$
 $\eta = 1$

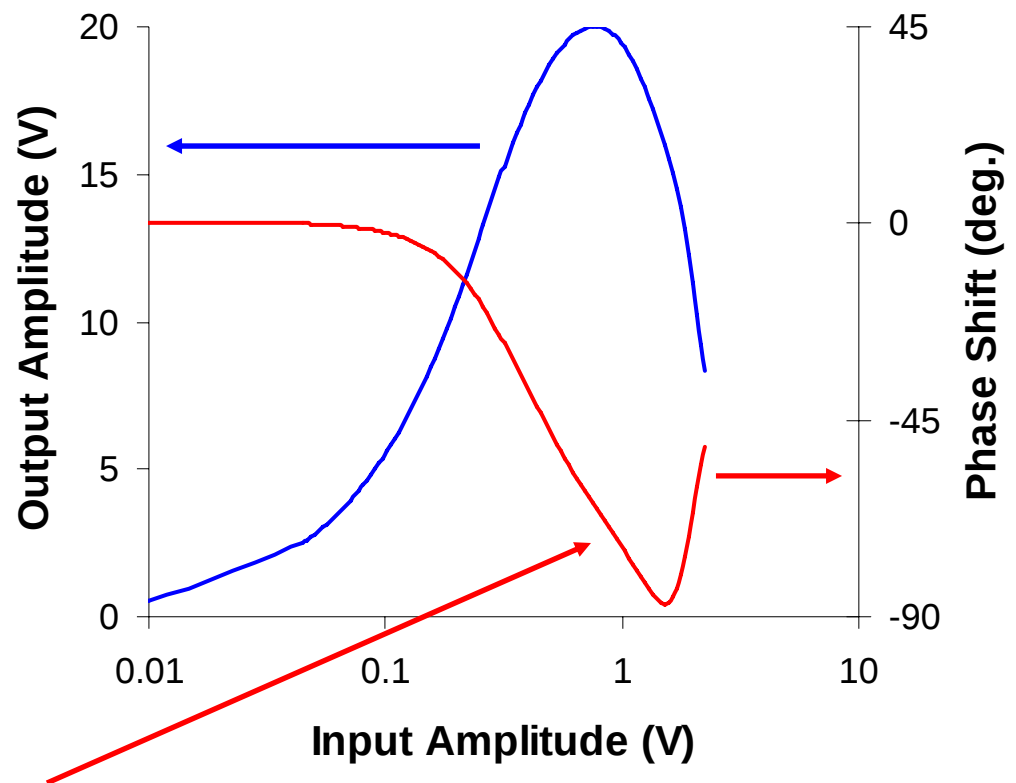


Return Map

Characteristics of 276HA TWT Driver Amplifier for Satellite Communications

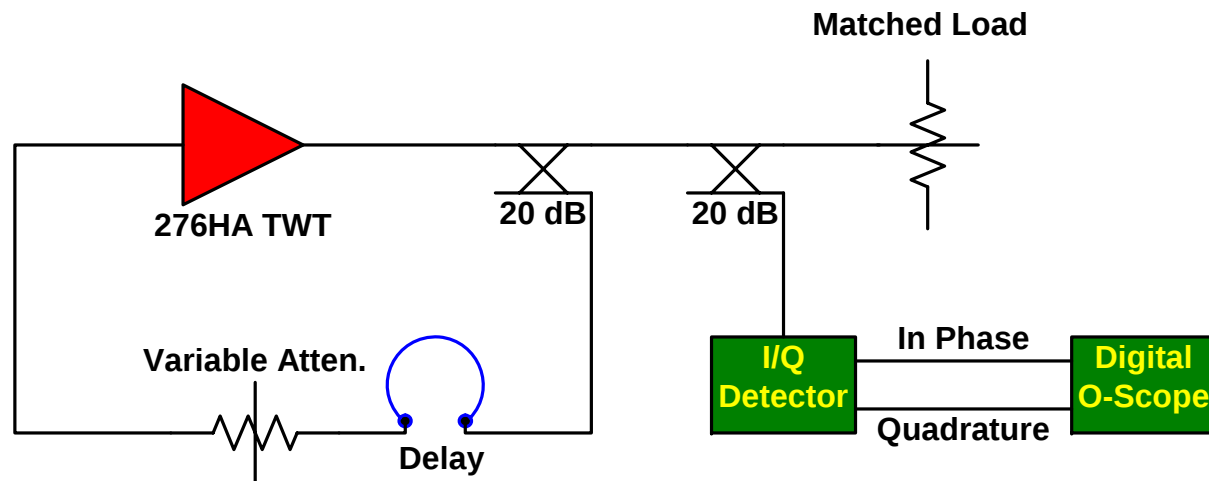
Frequency: 3-4 GHz
Output Power: 0.6 W
Gain: 35 dB
Bandwidth: 1 GHz
Efficiency: 70%

(Multi-Stage Depressed
Collector Design)



Phase becomes periodic for large input amplitudes!

Time-delayed Feedback Oscillator Experiment (Wideband)



Model

$$\eta = 1.0$$

$$\tau_{Norm} = 0.530$$

$$k = 7.142$$

Experiment

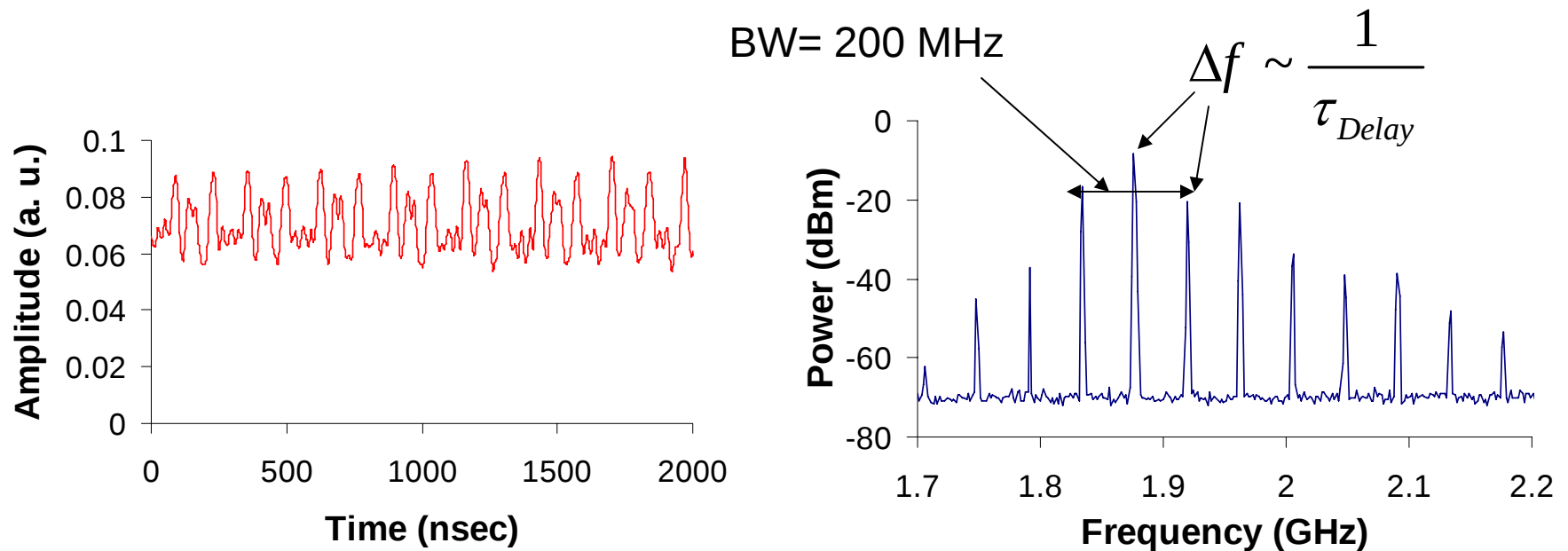
$$\eta = 3.4$$

$$\tau_{Norm} = (5\text{ ns})(2\pi * 1\text{ GHz}) = 10\pi$$

$$\Phi \neq \text{quadratic function of } |A_{in}|$$

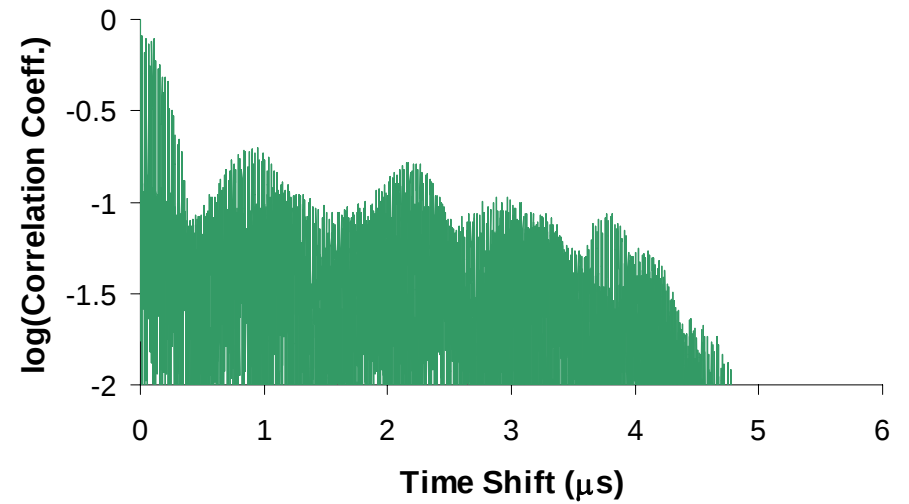
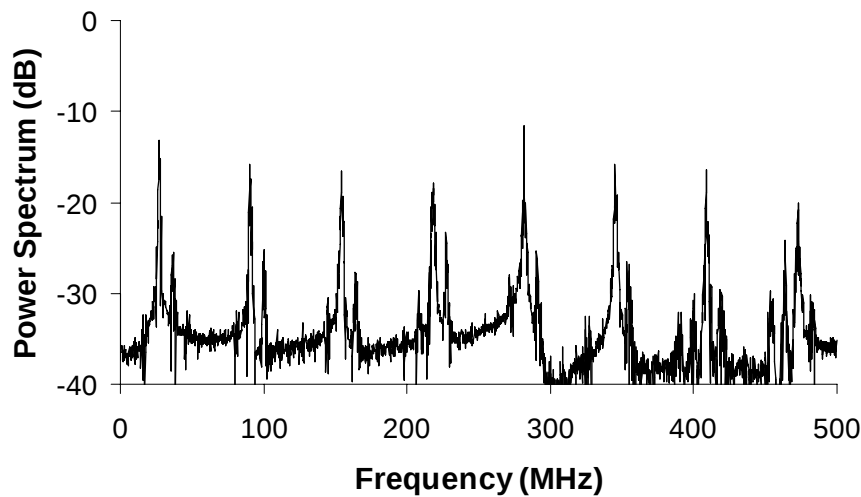
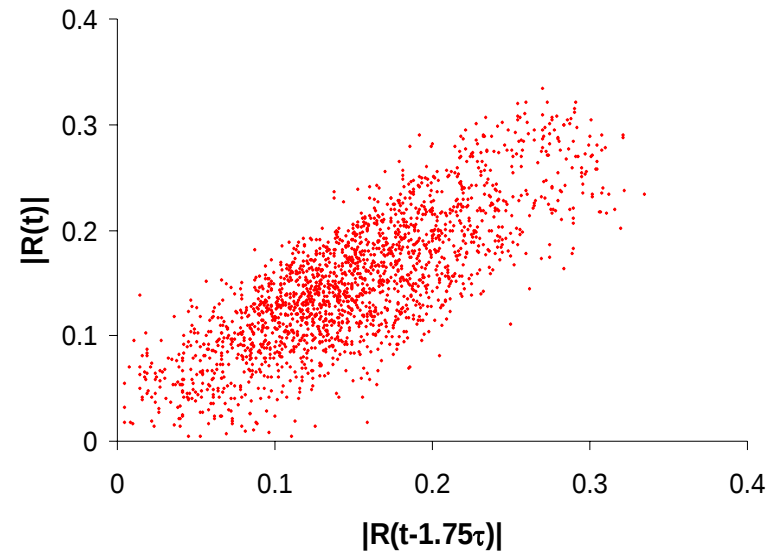
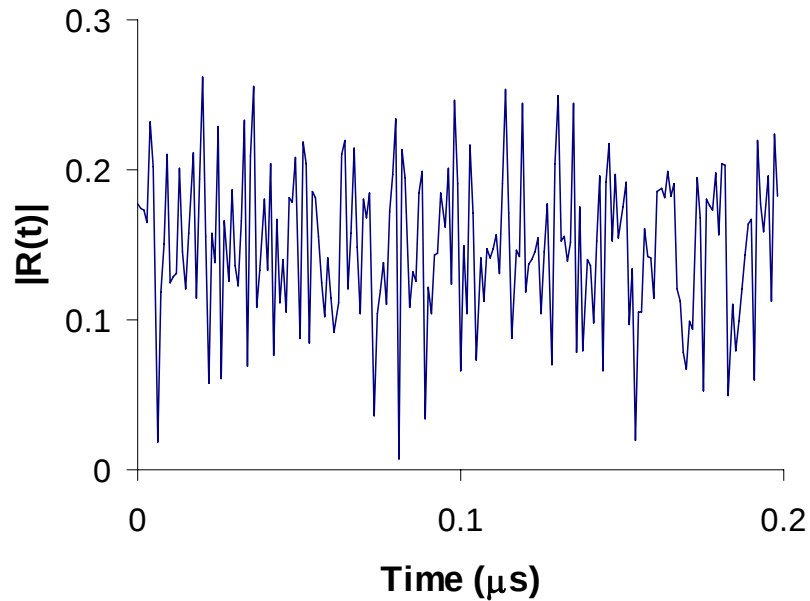
Caution: Our system has much longer memory!

Typical quasi-periodic behavior at low loop gains

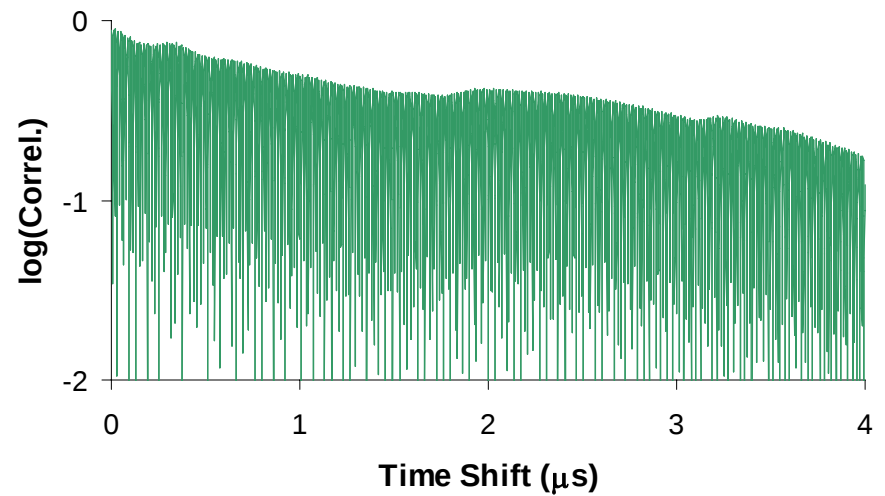
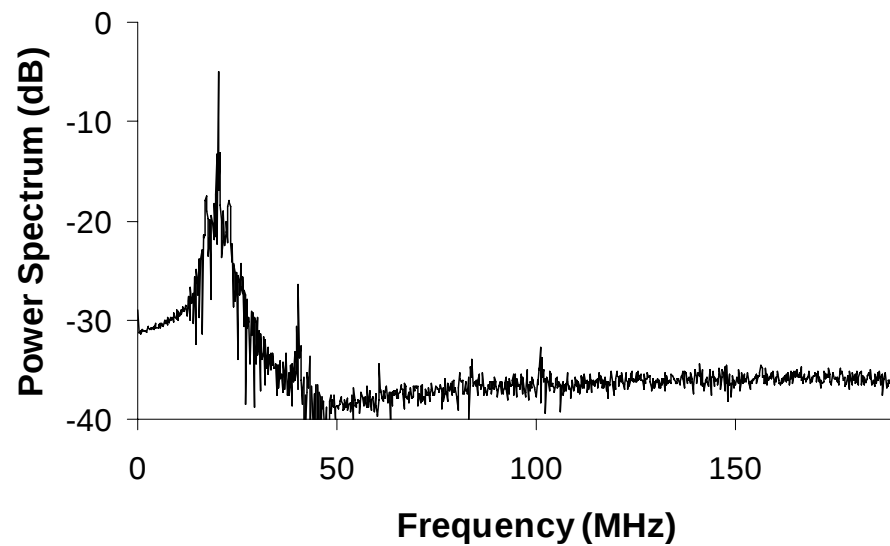
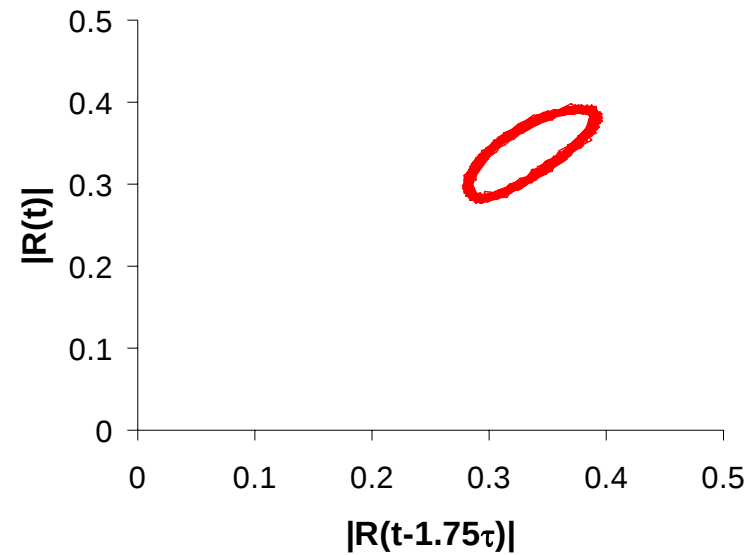
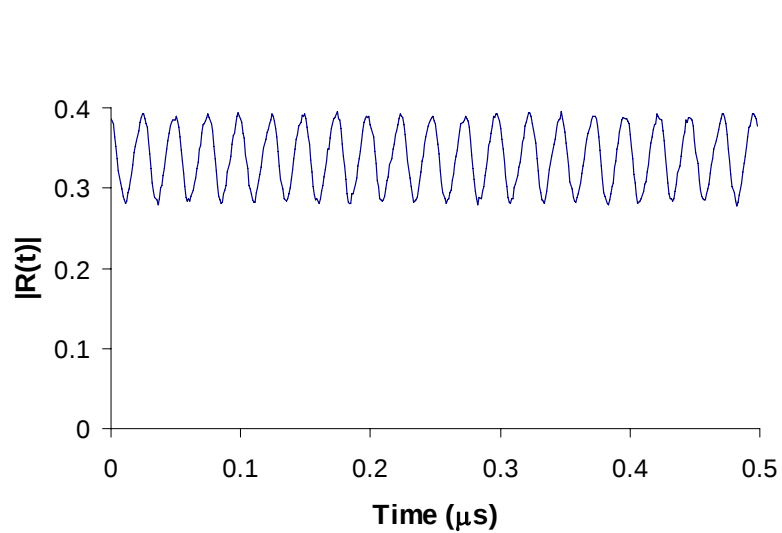


Experimental results from an L-band TWT with a short feedback delay ($\tau_D = 20$ ns).

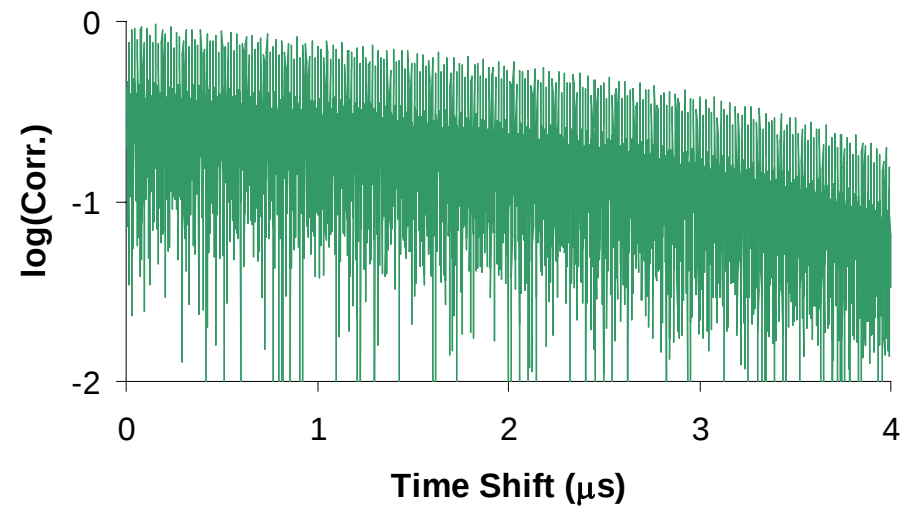
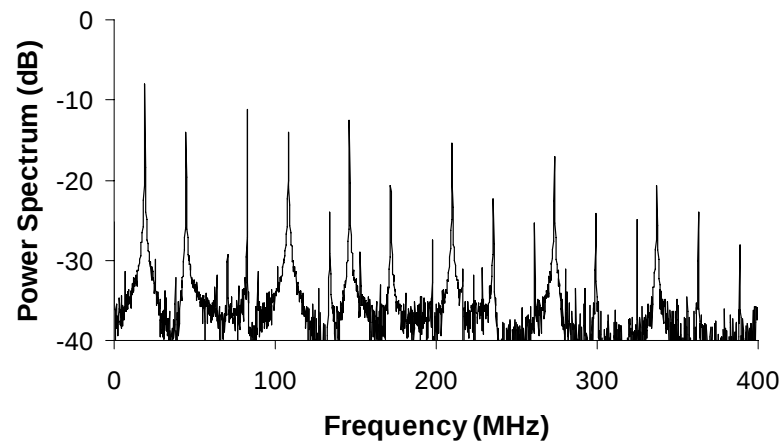
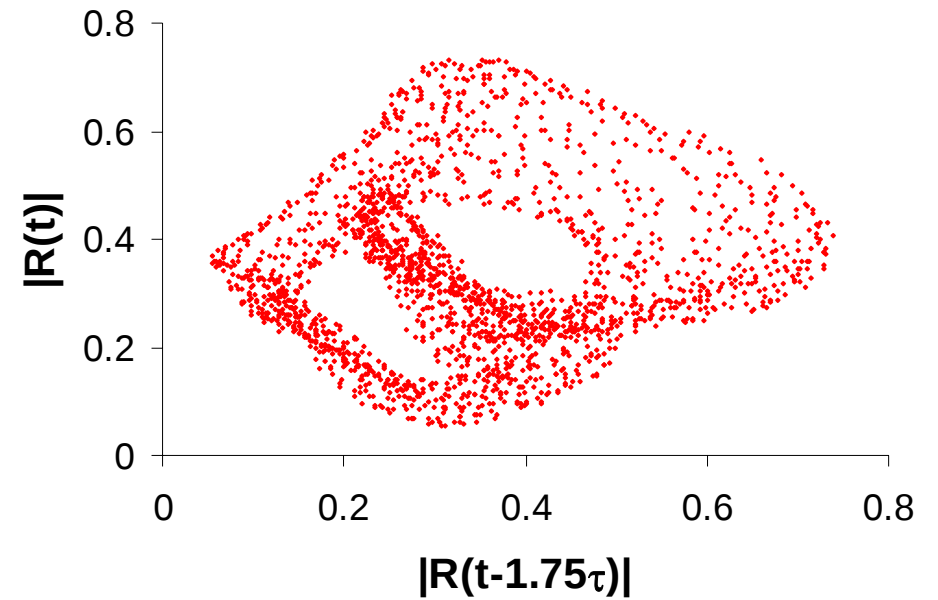
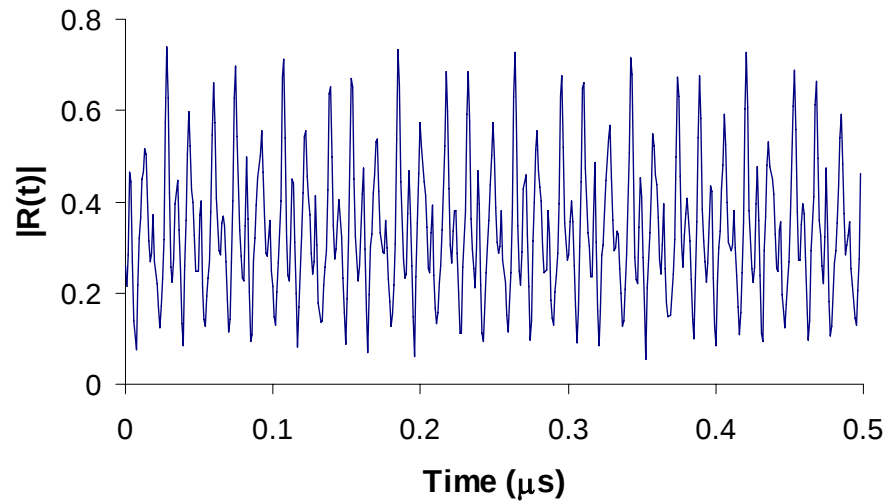
Full Band Case: Loop Gain, $k = 1.12$



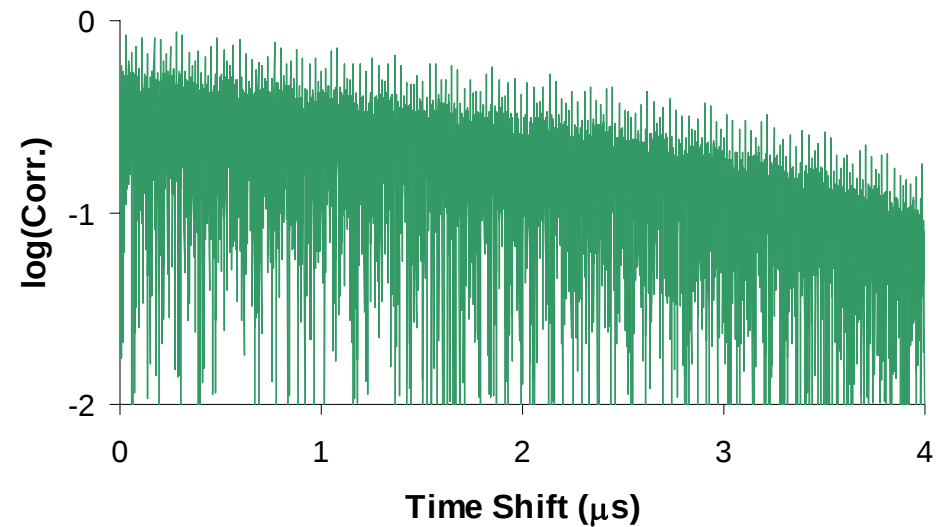
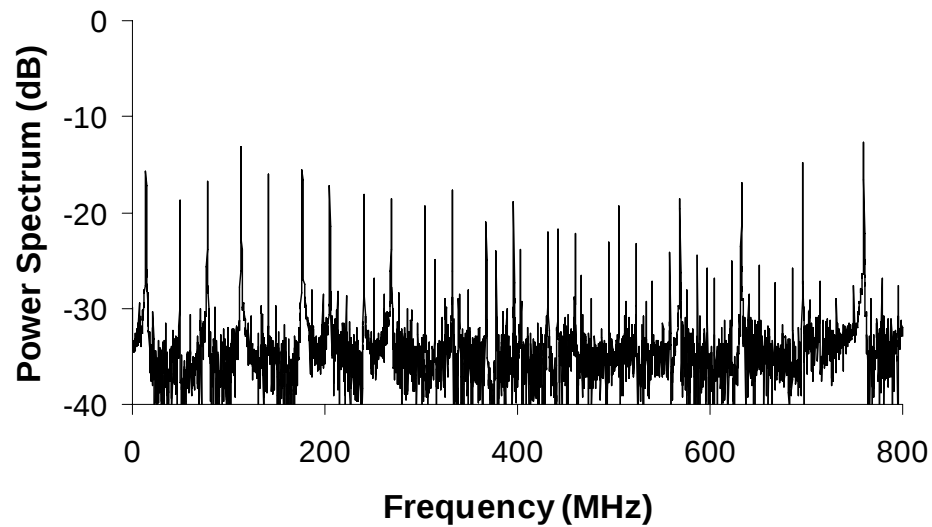
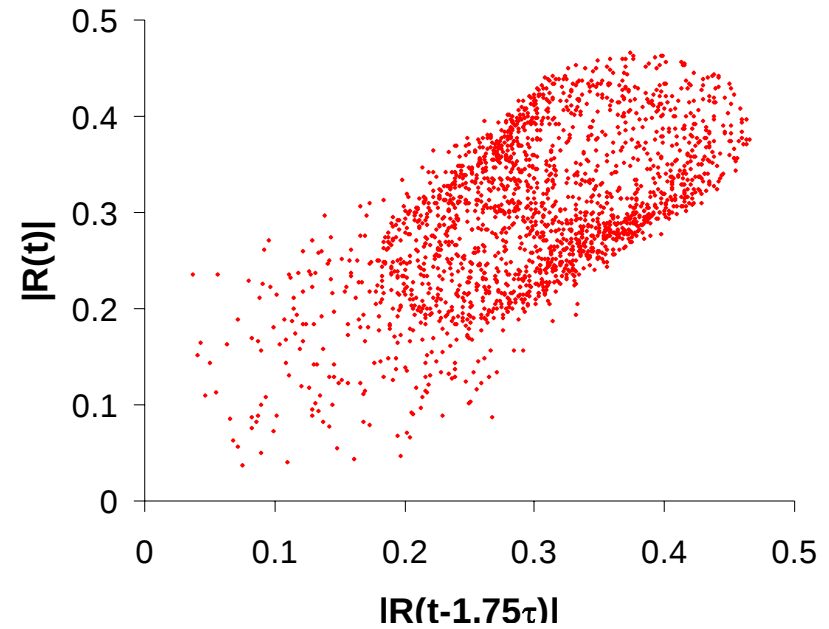
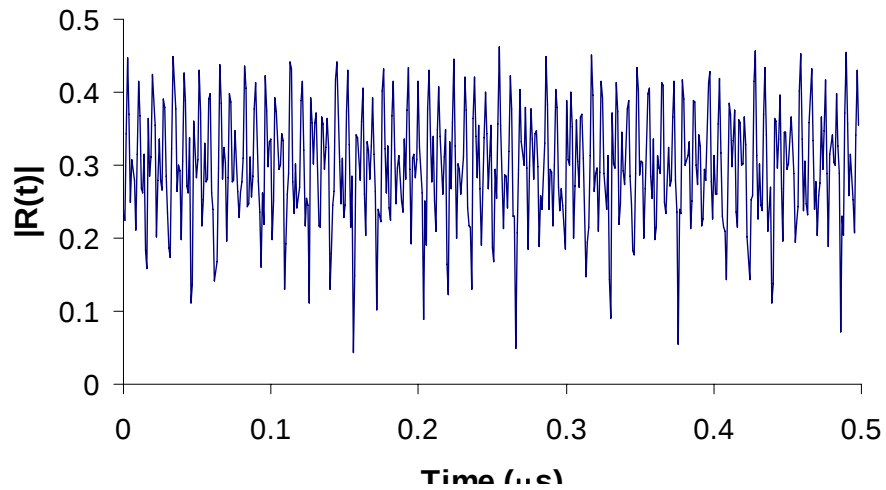
Loop Gain, $k = 1.41$



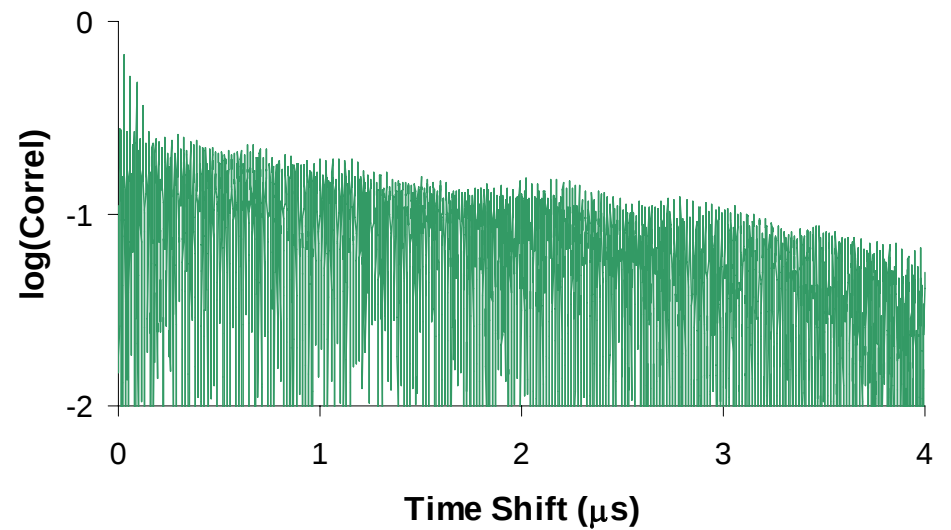
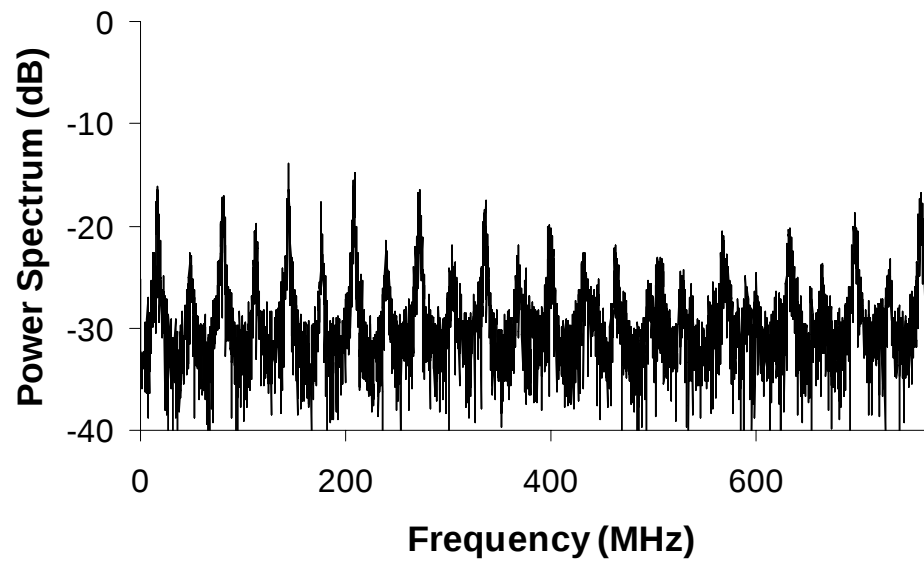
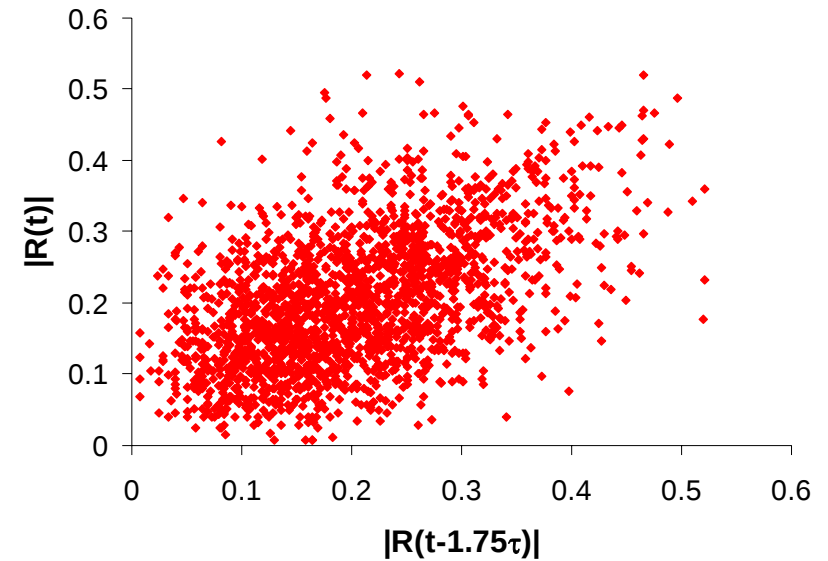
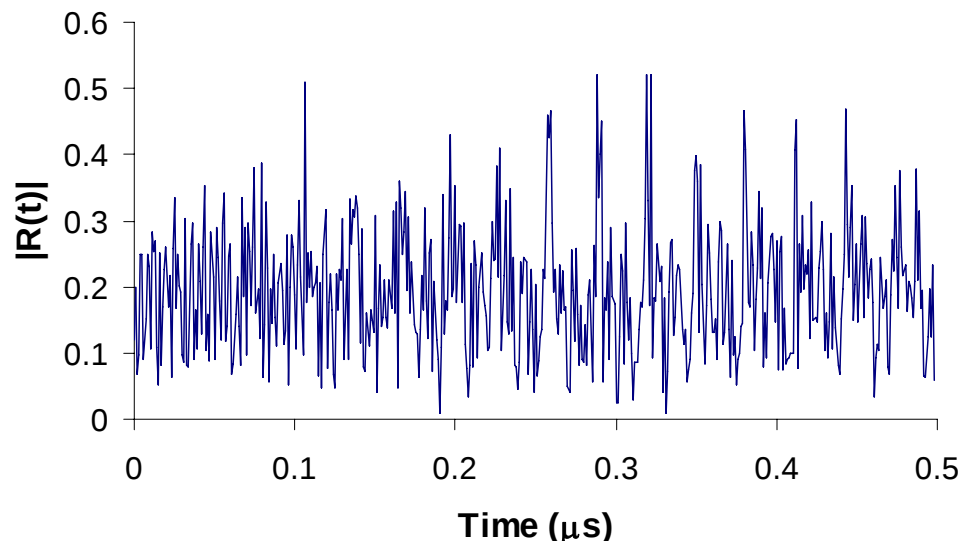
Loop Gain, $k = 1.60$



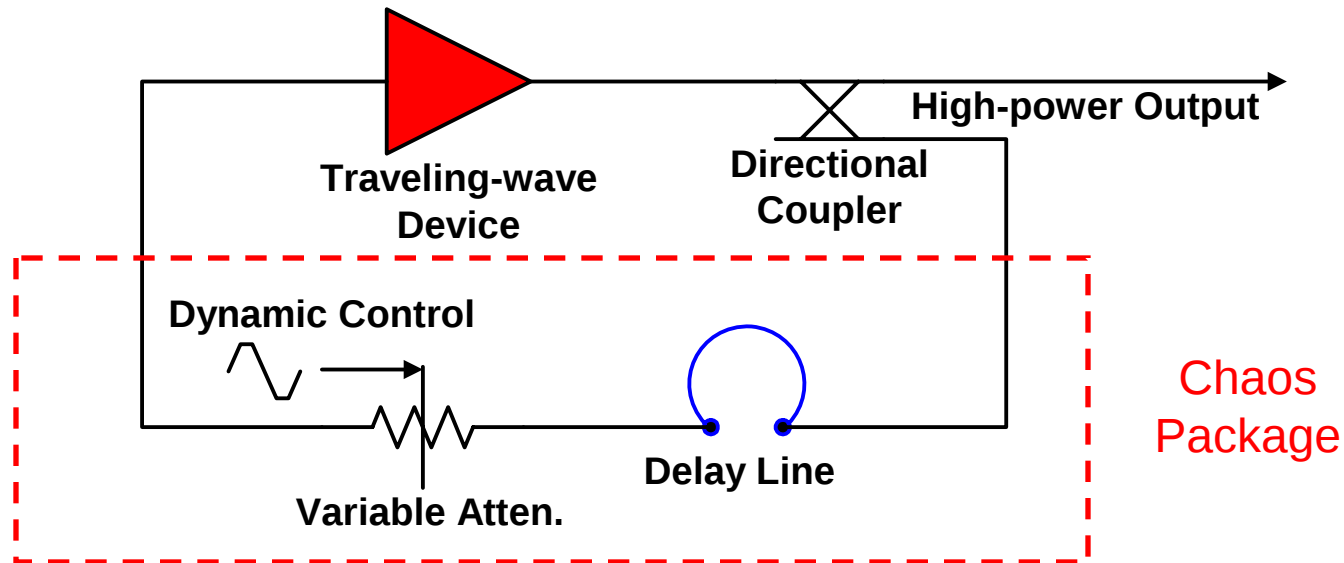
Loop Gain, $k = 4.0$



Loop Gain, $k = 7.94$

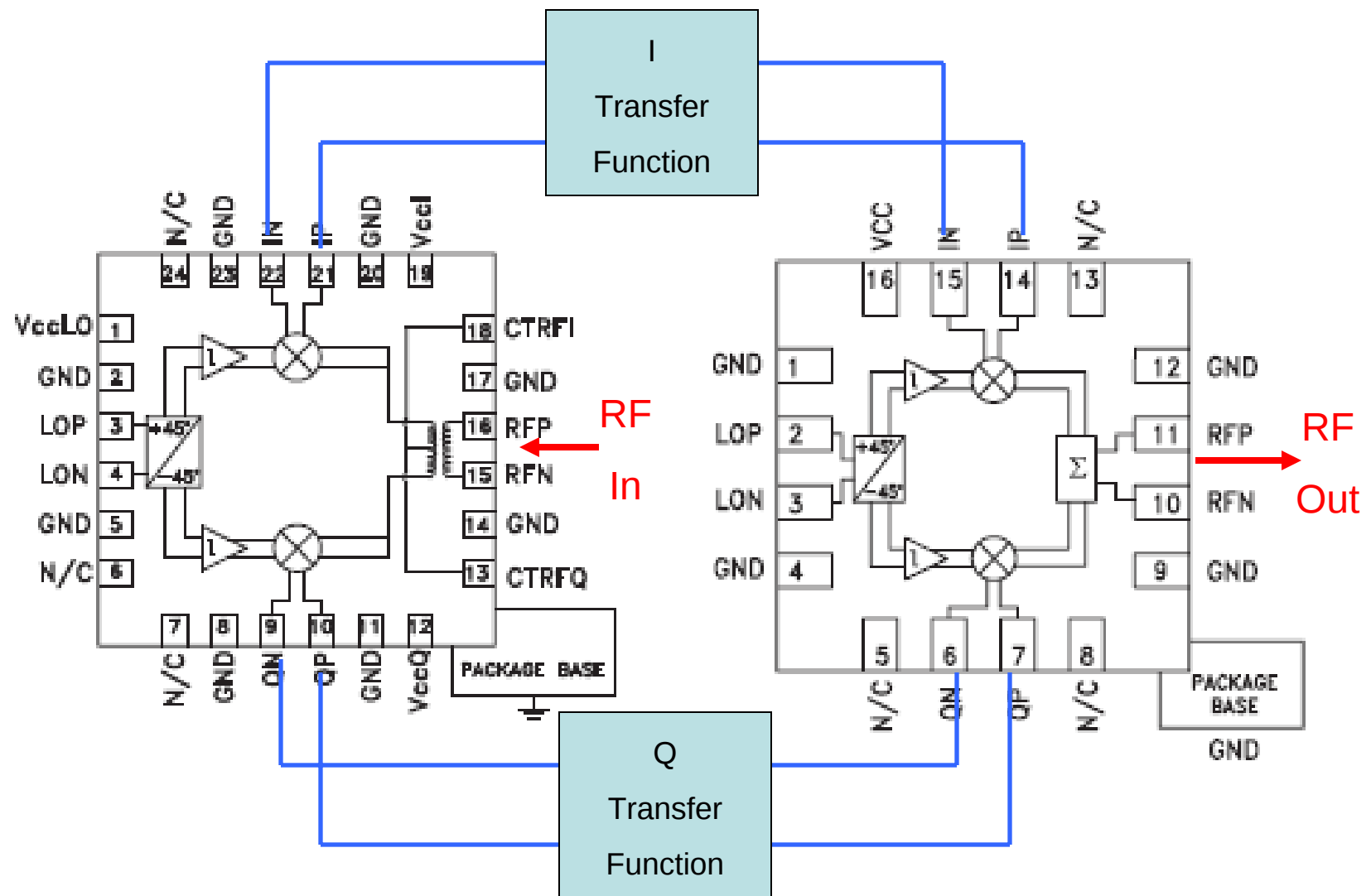


Deliverable: Develop an “dynamics package” that could be integrated into existing RF transmitters

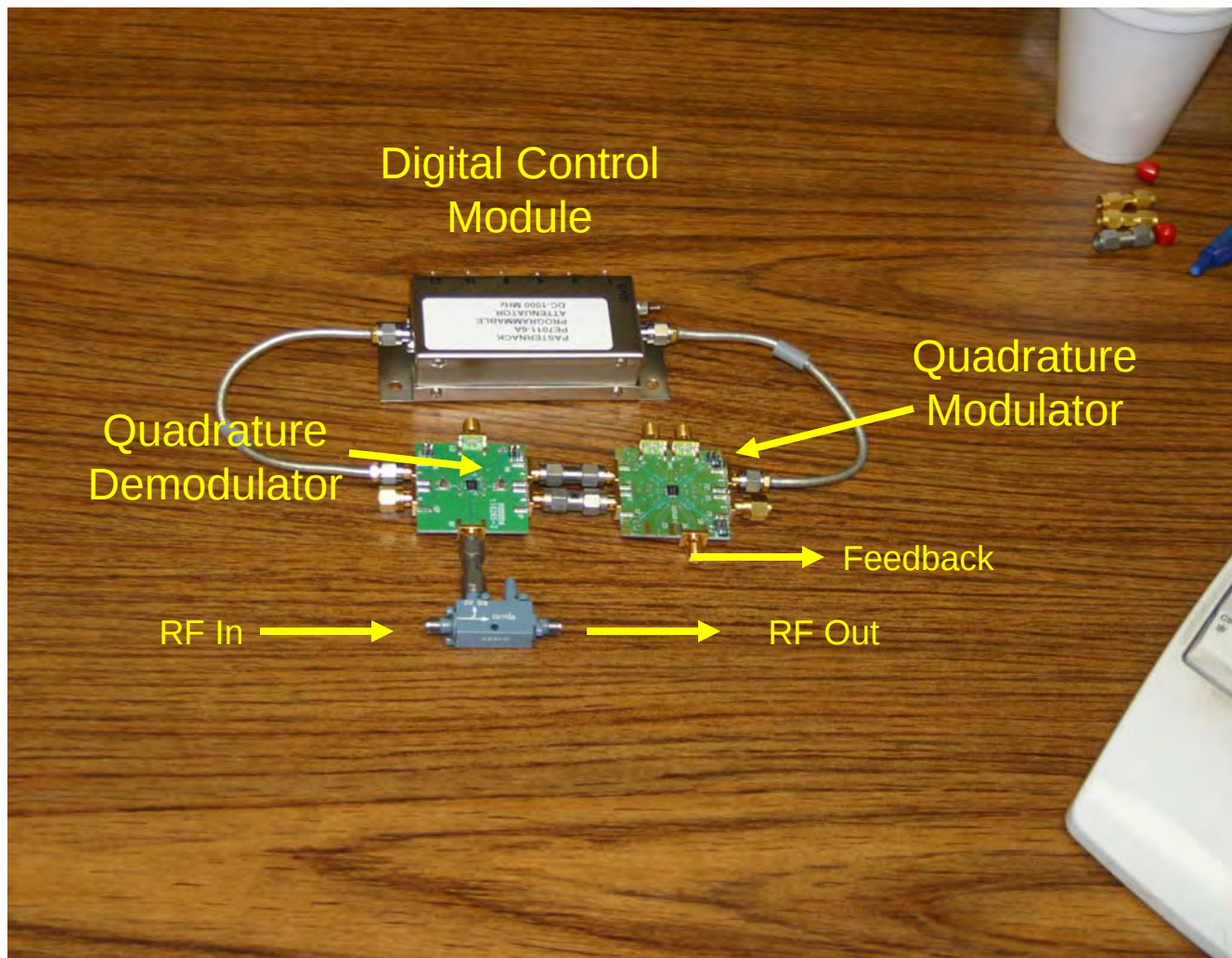


- Simple construction
- Uses existing technology that is deployed in a wide variety of military systems.
- Generates power levels and frequencies that would be useful for covering wide areas (e. g. urban environments).

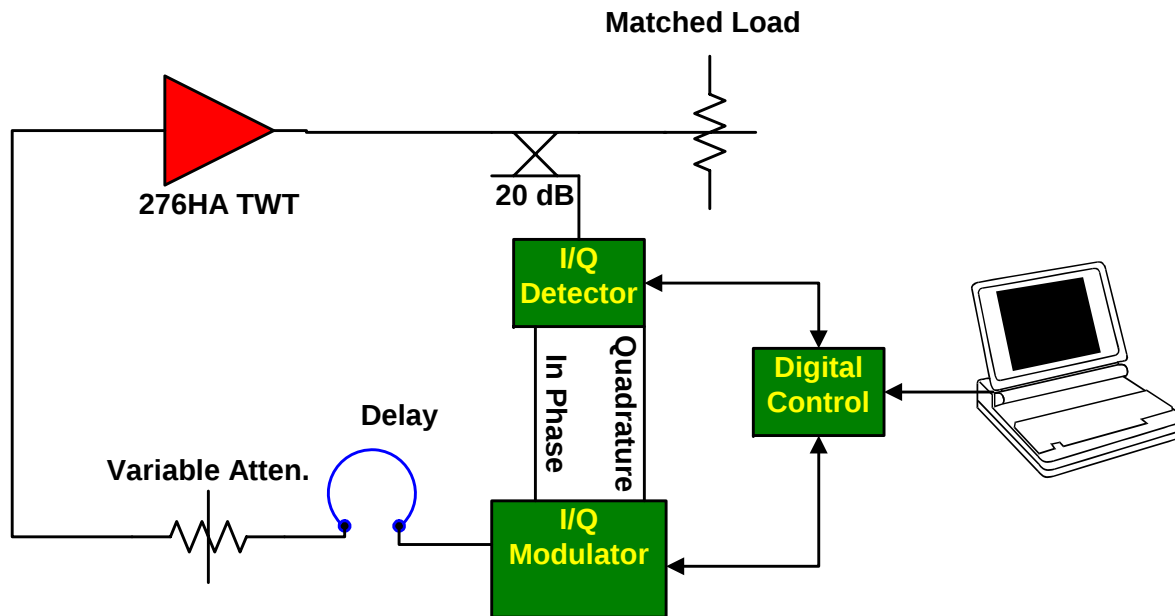
Digital control of dynamical states using quadrature feedback



Components of the dynamics control package



Digital Control of System State



- Adjustable loop gain/dynamics
- Apply new transfer functions to the feedback
- Automated setup of dynamics

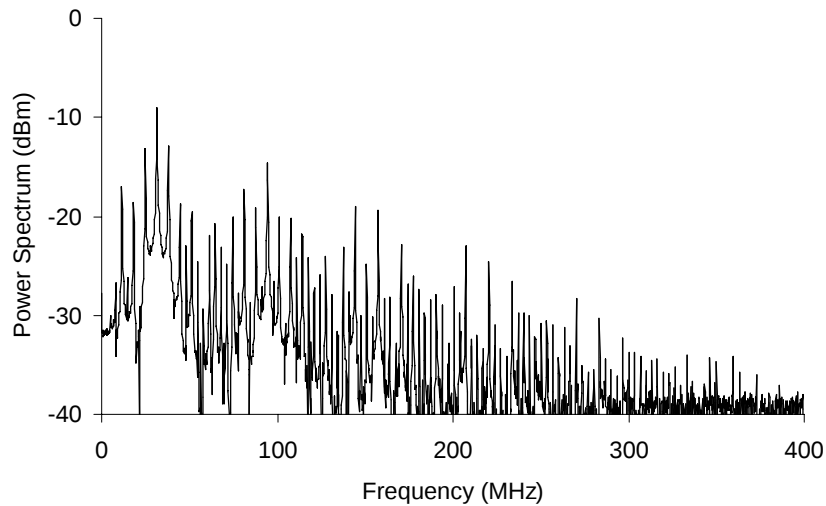
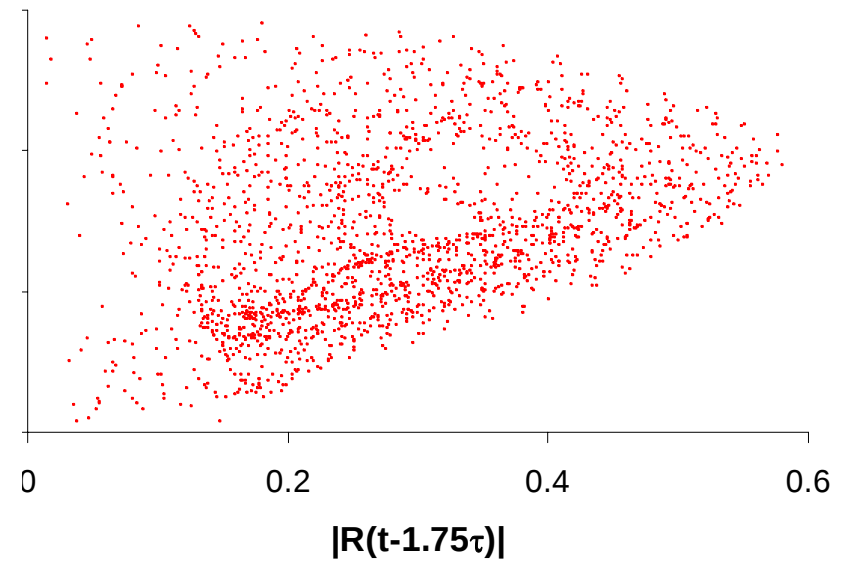
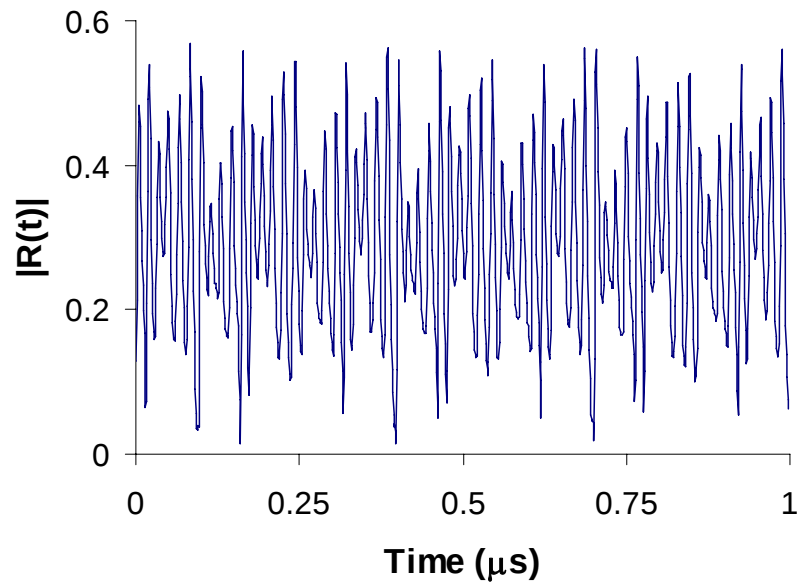
$$s = \pm I \pm iQ$$

$$s = \bar{s}$$

$$s = I^n \pm iQ^n$$

$$s = I \rightarrow Q, Q \rightarrow I$$

Complex Feedback Transfer Functions



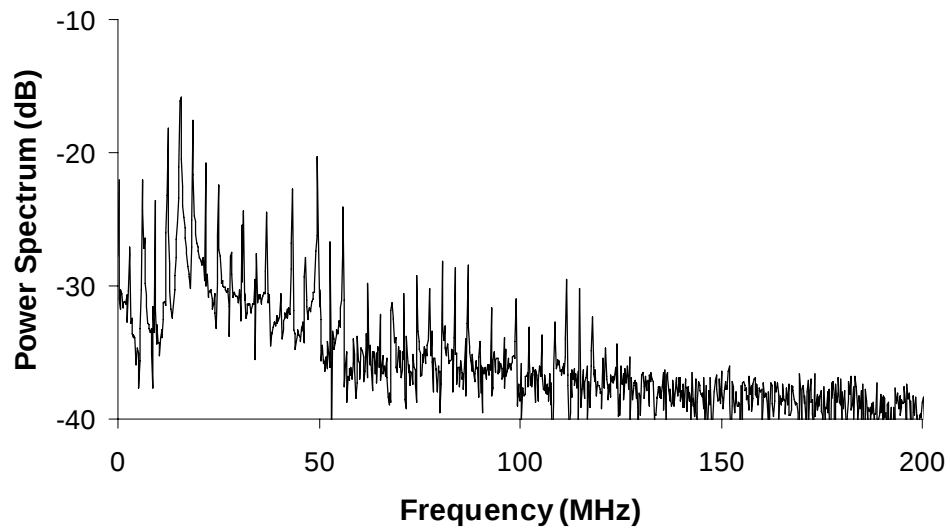
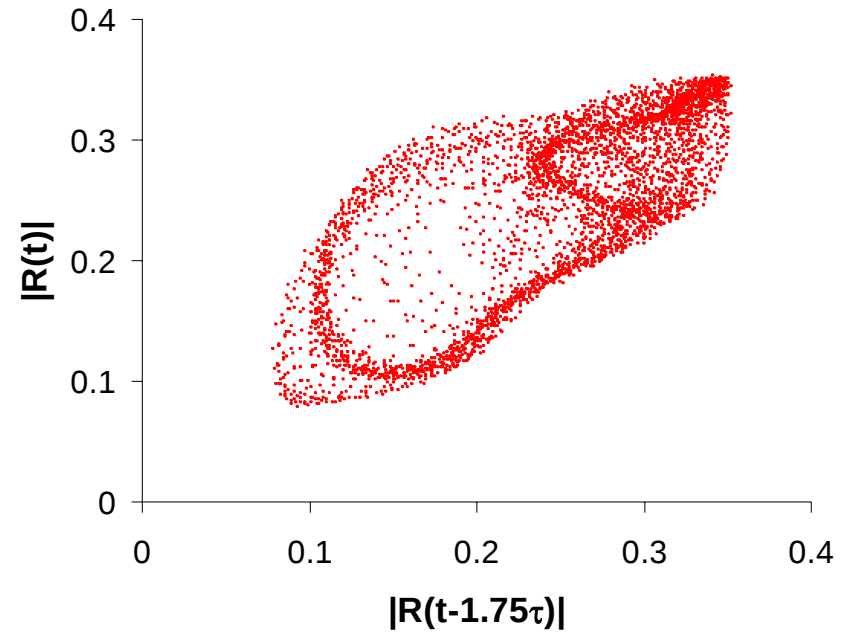
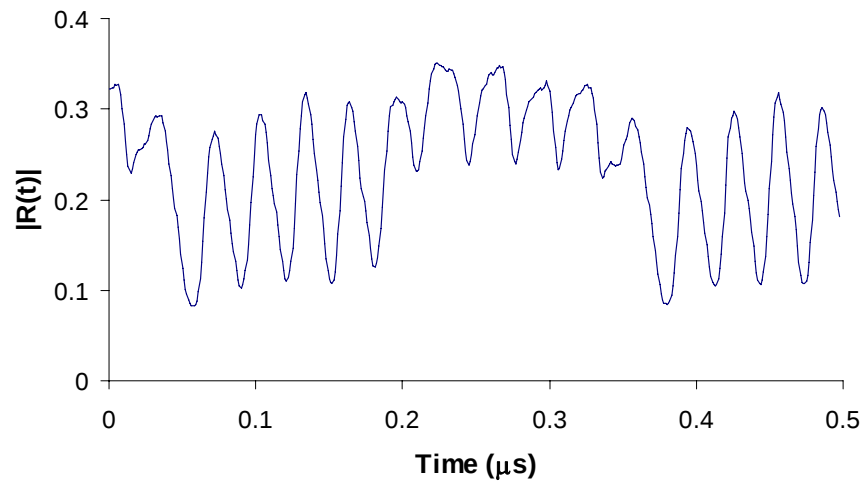
$$s = \bar{s}$$

$$\Delta\omega = 2\pi(40 \text{ MHz})$$

$$\tau_{Norm} = 1.25$$

$$k = 2.88$$

Complex Feedback Transfer Functions

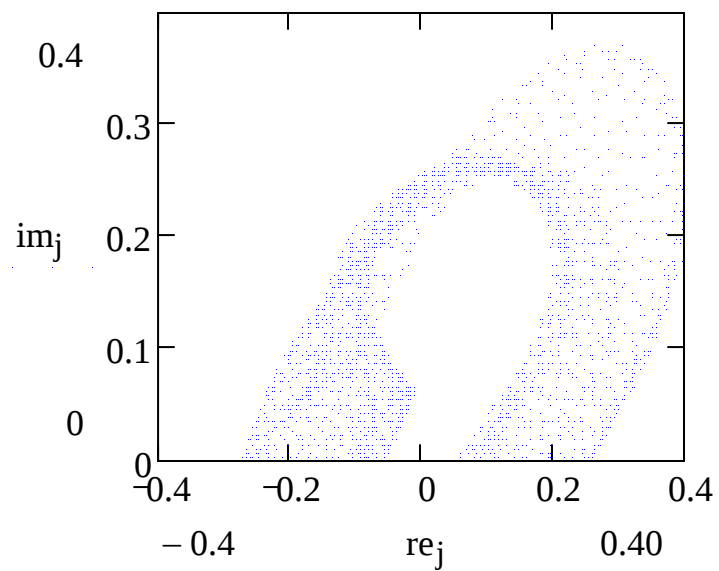
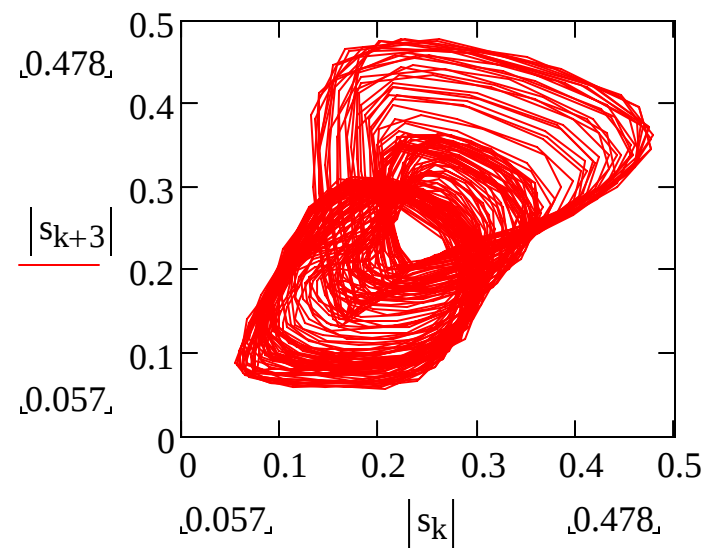
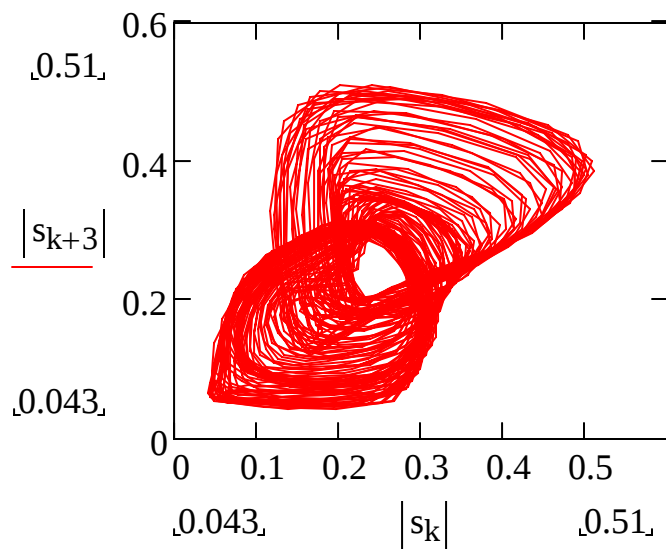


$$S = -S$$

$$\Delta\omega = 2\pi(40 \text{ MHz})$$

$$\tau_{Norm} = 1.25$$

$$k = 5.01$$



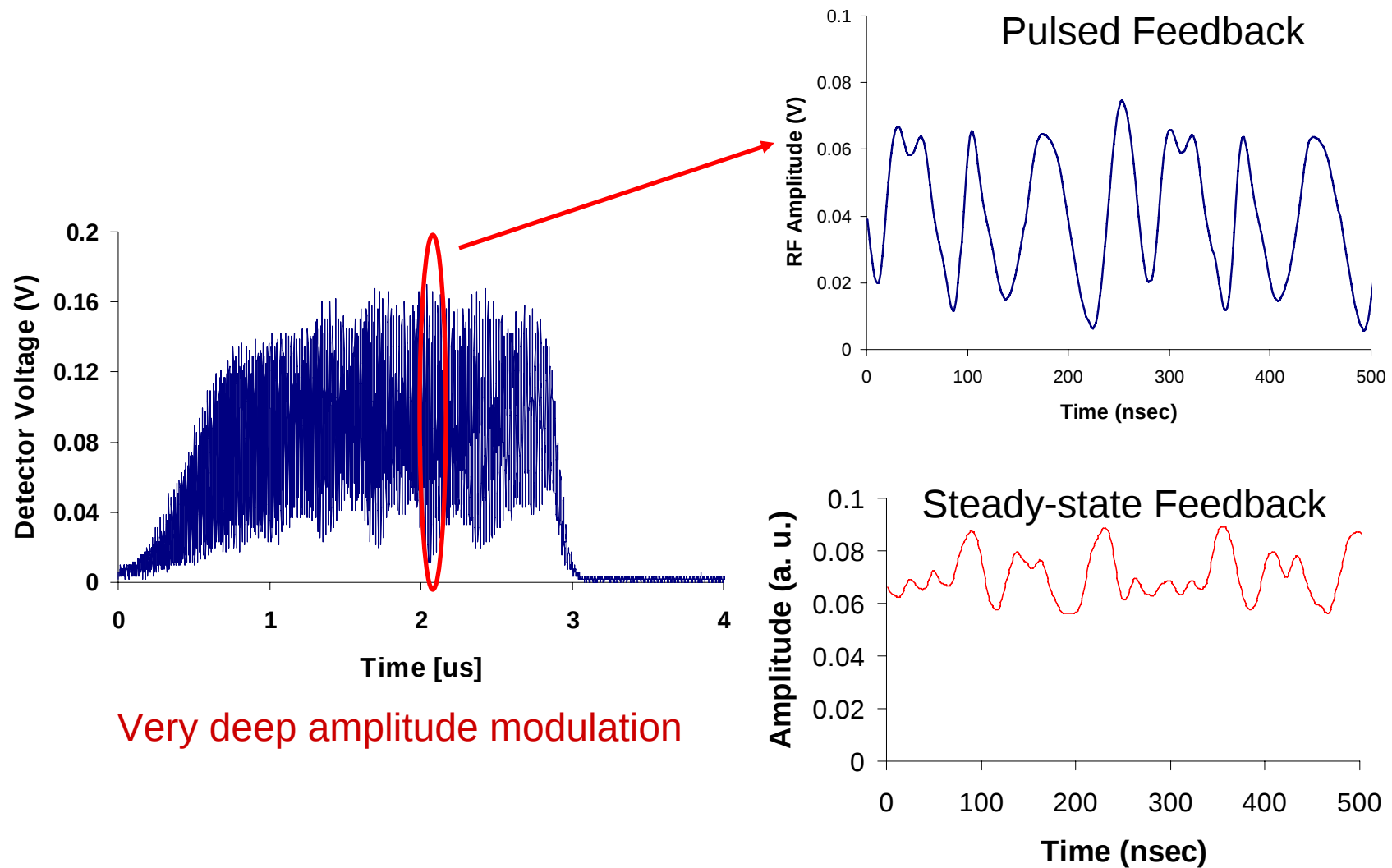
$$s = I - iQ$$

$$\Delta\omega = 2\pi(40 \text{ MHz})$$

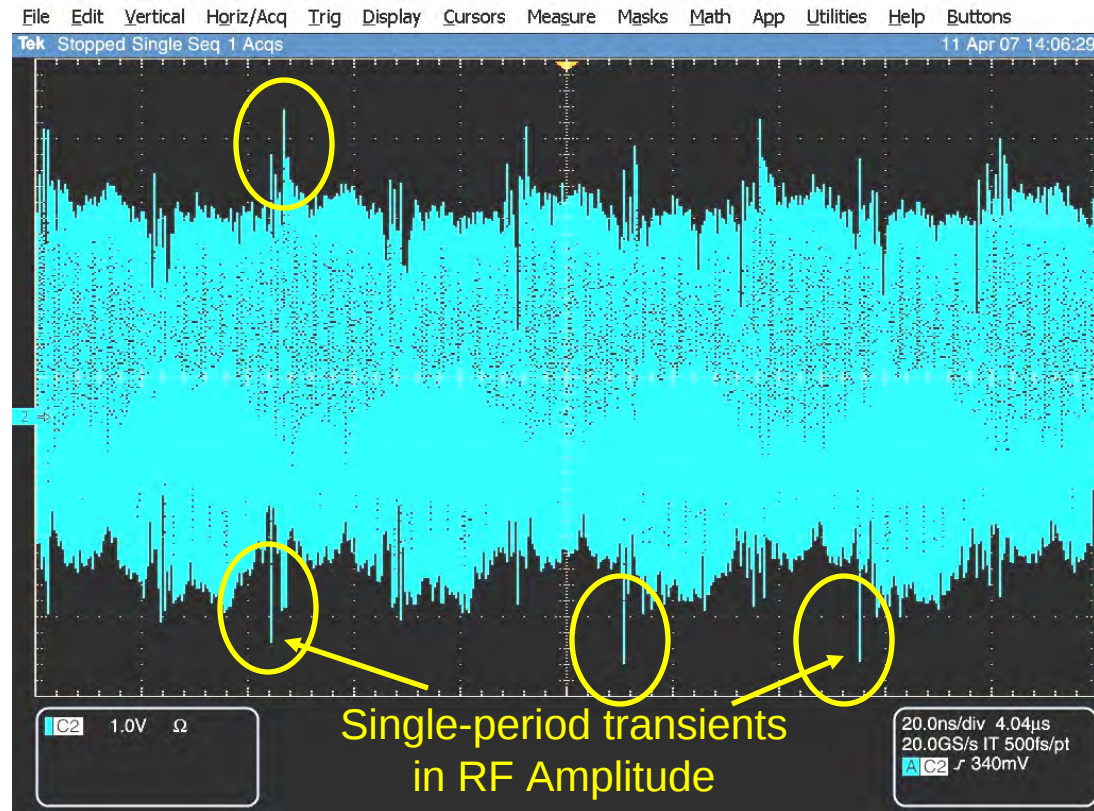
$$\tau_{\text{Norm}} = 1.25$$

$$k = 2.2, 5.01$$

Transient chaos in a TWT (pulsed beam or feedback)



- Transients in TWT TDO's



Time series of chaotic TWT output voltage
(measured)

Summary of 2008 Results

- Basic characterization of TWT TDO's at frequency bands relevant to Navy hardware:
 - L-band (1-2 GHz)
 - C-band (3-4 GHz)
 - X-band (8-12 GHz)
 - Ku-band (12-18 GHz)
- Demonstrated a simple method to control the state of the TWT TDO
 - Flexibility: the system can be adapted for various missions

Future Work (2009)

- Investigate synchronization in mutually coupled TWT TDO's
- Construct a network of TWT devices
 - Demonstrate digital state control of the network
 - Study network dynamics w/ static coupling
 - TDO network dynamics when coupled through complex, time-dependent environments