

## Air Hockey Implies Chaos – Kristen Casalenuovo

- I. Introduction
  - a. Chaotic scattering definition
  - b. Example of point particle in an electric field,  $b$  vs.  $\theta$  (*draw on board*)
  - c. What makes scattering chaotic is that for just small changes in  $b$ , there can be huge changes  $\theta$ .
  - d. Billiards – symbolic representation (frictionless, reflection) of chaotic scattering problem
  - e. We are extending this problem to cases with friction.
  - f. Thesis – With friction, there will be a significant difference in the output, but chaotic scattering will still occur.
- II. Friction Dynamics
  - a. Definition: force opposing tangential motion equal to coeff. of friction times the normal force.
  - b. Draw examples of varying friction forces and spins on board and demonstrate using tennis balls and super balls.
  - c. Collisions are not instantaneous, so...
- III. Impulse Force
  - a. Definition – change in force w.r.t. time (*draw integral on board*)
  - b. Assumption – when  $V_{\text{total}} = 0$ , the ball will roll, and the rolling friction is inconsequential. Thus no more change in motion.
  - c.  $V_{\text{net-before}} * V_{\text{net-after}} > 0$ . In these cases, we use locking impulse instead of the sliding impulse defined by the normal force.
  - d. Locking impulse – change in force until time ( $V_{\text{total}}=0$ ).
- IV. Research
  - a. Derived equations to define changes in forces during collisions with friction, translational velocity, and angular velocity.
  - b. Wrote Java program to examine data and to animate system.
  - c. We did find a significant difference in the output between cases with and without friction, and chaos still occurred.
  - d. For more information, visit me in the poster session.