Chaos and High Power RF Effects: Statistical Analysis of Induced Voltages



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AFOSR Presentation

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Goal



To develop a quantitative statistical understanding of induced voltage and current distributions in circuits inside complicated enclosures, based upon minimal information about the system

HPM Effects:



Electromagnetic Compatibility of Circuits





 Coupling of external radiation to computer chips is a complex process:

- Apertures
- Resonant cavities
- Transmission Lines
- Circuit Elements

System Size > Wavelength

We want to understand the scattering properties of this system including the effects of coupling

Statistical Distribution using Wave Chaos

Why Quantum / Wave Chaos?



Difficulty in making predictions of electromagnetic field structure in complicated enclosures

Predictions can depend sensitively on details

The "soda can problem"

Related work: (Field distributions in reverberation chambers, etc.)
R. Holland and R. St. John, *Statistical Electromagnetics* (Taylor and Francis, Philadelphia, 1999).
D. A. Hill *et al.*, IEEE Transactions on Electromagnetic Compatibility 36, 169 (1994).
L. K. Warne *et al.*, IEEE Trans. Antennas Propag. 51, 978 (2003).
and others...



The Difficulty in Making Predictions...





- 2 Dimensional Quarter Bow Tie Wave Chaotic cavity
- Classical ray trajectories are chaotic short wavelength Quantum Chaos
- 1-port, 2-port S and Z measurements in the 3-18 GHz range
- Ensemble average through 100 locations and orientations of the perturbations
- Perturbers are of size $\sim \lambda$ or bigger

Wave Chaotic Eigenfunctions





Uncover simple statistical properties of:

Eigen-frequencies, Eigen-functions, Scattering matrix, Impedance matrix, Admittance matrix, etc.

Many of these simple statistical properties are described by Random Matrix Theory

D. H. Wu and S. M. Anlage, Phys. Rev. Lett. <u>81</u>, 2890 (1998).

Practical Implications for Real Life Problems Bare Minimum Specifications for Induced-Voltage Statistics





What are the bare minimum specifications to accurately predict voltage Statistics?



Algorithm for Predicting Component Induced-Voltage Distributions:







Application of RCM to a Real Problem Induced Voltage PDFs in a Computer Enclosure and Room





Variance of Voltage and Current Distributions on the Target











Operational Statements:

Measure Var(Z₁₁) of the target to quantify its degree of susceptibility to HPM attack Minimizing Var(Z₁₁) of the target is a strategy for minimizing damage from HPM attack

Cavity Impedance and Field PDF Engineering **RCM Results** $P(\mathbf{R}_{cavity})$ (high loss) $Z_{cavity} = R_{cavity} + i X_{cavity}$ (intermediate loss) (low loss) 0.75 R_{Rad} sets the scale for R_{cavity} 0.5 Low-loss case: $R_{Cavity} < R_{Rad}$ 0.25 Lossy case: \Rightarrow Gaussian distribution, width ~ \sqrt{Q} **R**_{cavity} **R**_{radiation} 0 Ingress 2 **≜**|S₂₁| P(X_{cavity}) Gaussian (high loss) 1.2 $\Delta f_{3dB} >> spacing$ Ingress 1 width~ \sqrt{Q} 1 Lorentzian↔Gaussian 0.8 $|S_{21}|$ (intermediate loss) 0.6 width=R_{Rad} Std. Lorentzian (low loss) 0.4 0.2 $\Delta f_{3dB} \ll spacing$ **X**_{cavity} X_{Rad} sets the scale for X_{cavity} 0 X_{Rad} Low-loss case: broad tails, width ~ $R_{Radiation}$ Lossy case: narrow distribution, width ~ \sqrt{Q}

Conclusions



Deterministic measurements (or calculation/simulation) of the <u>radiation impedance</u> remove the effects of coupling to recover universal statistical electromagnetic properties

Experimental tests of many basic 1 port and 2-port predictions have confirmed that the approach is correct.

Frequency, Volume
$$\begin{cases} k^2 \\ \Delta k_n^2 Q \end{cases}$$
 Determine the Z, S PDFs
Radiation impedance of the ports

Proposed a universal relation for impedance variances in 2-port systems

Clear strategies to engineer the PDFs to suit one's purpose

S. Hemmady, *et al.*, Phys. Rev. Lett. <u>94</u>, 014102 (2005) X. Zheng, *et al.*, J. Electromag. <u>26</u>, 3 (2006) X. Zheng, *et al.*, J. Electromag. 26, 37 (2006) S. Hemmady, *et al.*, Phys. Rev. E <u>71</u>, 056215 (2005) X. Zheng, *et al.*: submitted to Phys. Rev. E, cond-mat/0504196

Our Vision for the Future...



• Random Coupling Model shows very promising signs... But still in its infancy.

- Experimentally Validate RCM in realistic 3D environments:
- GENEC device
- Mode-Stirred Chambers at ONERA
- Realistic antenna configurations (apertures, bundle of cables, etc.)
- Non-Reciprocal Media as a way to mitigate EM "Hot Spots" –Darmstadt-Germany

• Transfer the Model and it's predictive capabilities to the END User:

- Document the strengths and weaknesses of the model
- Demonstrate it's utility (User's Guide)
- Educate the User in the strategy and execution of predictions
- Extend RCM to Pulsed Time-Domain Measurements:
 - Compelling Theoretical Work initiated Hart, Antonsen, Ott
- Connect RCM to the EM Topology Approach: •Quantum graphs and chaos on networks

GENEC Hardware







Vo

EMC Topology and CRIPTE- Baum, Liu, Tesche, Parmantier



Aircraft and cable configuration







• For really complex systems, a small change in frequency, orientation of EM features can result in vastly different internal field configurations.

•Need for a Statistical Approach

⁺₇Parmantier, J-P-*IEE Computing & Control Engineering Journal*, April 1998.

Some Other Future Plans



Consider the effects of objects inside the enclosure



SCARS (Heller, 1984)

Concentrations of wave density along unstable periodic orbits.

Quantum counterpart to classical phase space density is not uniform on the energy surface.

Study of <u>mixed</u> dynamics (Chaotic and regular)

What can be done with Time-Reversed Electromagnetics?

Deliver a localized "Electromagnetic Punch"



Transmit mode