

Comparing simulation of plasma turbulence with experiment

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The direct quantitative correspondence between theoretical predictions and the measured plasma fluctuations and transport is tested by performing nonlinear gyro-Landau-fluid simulations with the GRYFFIN (or ITG) code [W. Dorland and G. W. Hammett, *Phys. Fluids B* **5**, 812 (1993); M. A. Beer and G. W. Hammett, *Phys. Plasmas* **3**, 4046 (1996)]. In an *L*-mode reference discharge in the DIII-D tokamak [J. L. Luxon and L. G. Davis, *Fusion Technol.* **8**, 441 (1985)], which has relatively large fluctuations and transport, the turbulence is dominated by ion temperature gradient (ITG) modes. Trapped electron modes and impurity drift waves also play a role. Density fluctuations are measured by beam emission spectroscopy [R. J. Fonck, P. A. Duperrex, and S. F. Paul, *Rev. Sci. Instrum.* **61**, 3487 (1990)]. Experimental fluxes and corresponding diffusivities are analyzed by the TRANSP code [R. J. Hawryluk, in *Physics of Plasmas Close to Thermonuclear Conditions*, edited by B. Coppi, G. G. Leotta, D. Pfirsch, R. Pozzoli, and E. Sindoni (Pergamon, Oxford, 1980), Vol. 1, p. 19]. The shape of the simulated wave number spectrum is close to the measured one. The simulated ion thermal transport, corrected for $\mathbf{E} \times \mathbf{B}$ low shear, exceeds the experimental value by a factor of 1.5 to 2.0. The simulation overestimates the density fluctuation level by an even larger factor. On the other hand, the simulation underestimates the electron thermal transport, which may be accounted for by modes that are not accessible to the simulation or to the BES measurement.

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I. INTRODUCTION AND SUMMARY

There is much indirect evidence that low frequency turbulence driven by plasma gradients is responsible for anomalous transport in the core of tokamak plasmas.^{1,2} This evidence is obtained both from theoretical or numerical predictions of energy transport and its scaling and from experimental correlation between transport and turbulence levels.^{3–8} In particular, shear in the radial electric field has been associated with reduction in the turbulence levels and the improvement of confinement.^{9,10} Evidence for flow-shear suppression of the turbulence has also been obtained in global gyrokinetic simulations.⁸ Nevertheless, the direct quantitative correspondence between the theoretical predictions and the measured fluctuations and transport has not been established in the plasma core.

Here, we investigate this connection by performing

nonlinear gyro-Landau-fluid (GLF) simulations using the GRYFFIN (or ITG) code^{11,12} and comparing the results with data from a particular reference discharge on the DIII-D tokamak.¹³ Each simulation predicts simultaneously the transport fluxes (of both energy and particles) and the amplitudes and spectral properties of the turbulence at a particular time and radial position. If all these quantities can be shown to agree with the data, then this exercise will help to establish the validity of the anomalous transport theory and the causal relationship between the turbulence and the transport. If we could subsequently make accurate predictions for a wide range of different conditions, then the theory would be strongly supported. (A complete theory of transport in tokamaks would also have to account for transient phenomena that are difficult to describe within a conventional diffusive-convective framework.^{14–17} We do not address this question here.)

We presume the turbulence in question to be of the drift-wave type, including ion temperature gradient (ITG) modes,

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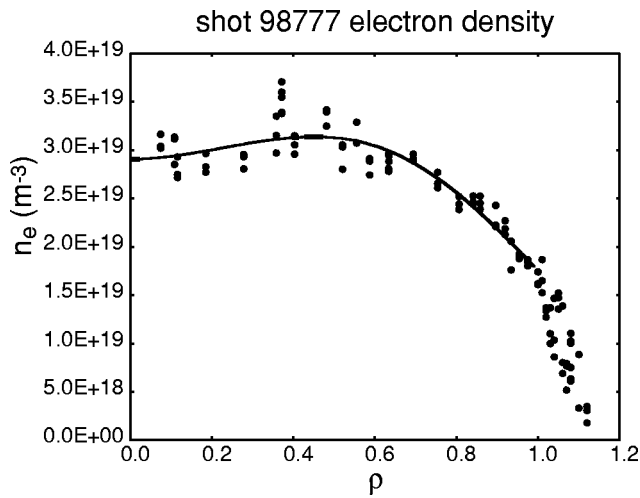


FIG. 1. Electron density data and profile fit from Thomson scattering.

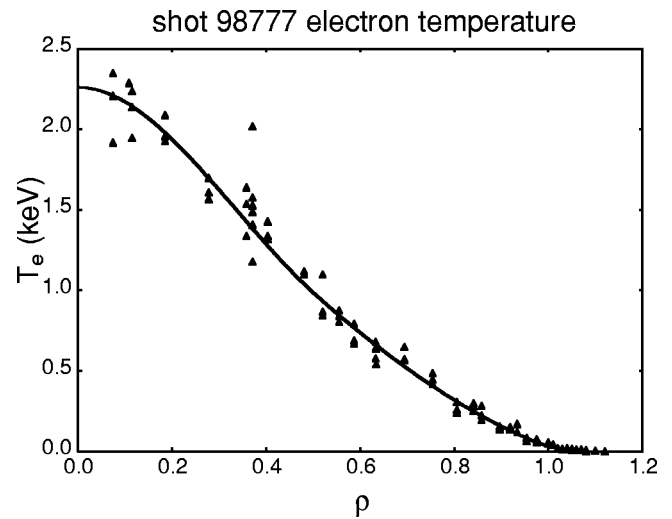


FIG. 3. Electron temperature and profile fit from Thomson scattering.

trapped electron modes, and impurity drift waves. These long wavelength ($k \leq 2.5 \text{ cm}^{-1}$) fluctuations are measured by beam emission spectroscopy (BES)^{18–20} and simulated by the code. Electron temperature gradient (ETG) modes, which cannot be resolved by either the BES or this code may also be important for the transport, especially that of the electrons.^{21,22} Transport fluxes and corresponding thermal and particle diffusivities are obtained from power and particle balance analysis as determined by the TRANSP code.²³ Measured density and temperature profiles used in the TRANSP analysis also make up part of the input to the simulation code. Likewise, the geometry used in both the analysis and the simulation is derived from fits to the equilibrium produced by the EFIT code.²⁴

The comparison requires correcting the simulation results for the measured $\mathbf{E} \times \mathbf{B}$ flow shear, which we do using a “quench rule” proposed by Waltz *et al.*²⁵ Similarly, the interpretation of the BES measurement requires accounting for the sample volume, which filters the higher wave-number modes.^{26,27} Even with these corrections we find that the simulated thermal ion transport exceeds the measured value by a factor of 1.5 to 2.0 depending on the choice of flow-

shear correction. The shape of the wave-number spectrum is close to the measured one, but the density fluctuation level \tilde{n}_e/n_e exceeds the BES measurement by a factor of 4 or 5. On the other hand, the electron thermal flux is smaller than that of the experiment. We speculate that the missing electron transport is accounted for by some other turbulent mechanism, e.g., the ETG modes.

Our principal difficulty is to account for the overestimate of the ion transport and the even larger overestimate of the fluctuation level. The latter is particularly hard to understand, since we expect the transport fluxes to be proportional to \tilde{n}_e^2 . We believe that errors in the BES measurement are far too small to account for this discrepancy. A major source of uncertainty in this work is that of the local gradients, especially the effects of impurities. We have presented a preliminary survey of these effects elsewhere.²⁸ Gyrokinetic simulations have been shown to exhibit an upward nonlinear shift in the temperature gradient threshold, which could, together with the temperature gradient uncertainty, alleviate the discrepancy.^{29,30} For the conditions considered here, how-

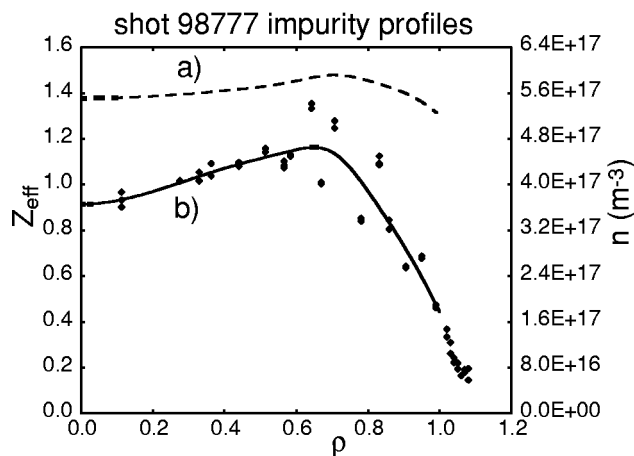
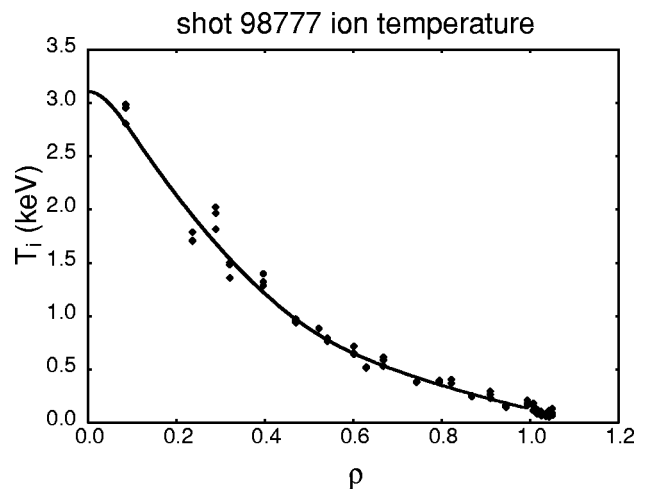
FIG. 2. (a) Z_{eff} (left-hand scale) and (b) carbon density data points and fit (right-hand scale).

FIG. 4. Ion temperature data and profile fit from charge-exchange recombination spectroscopy.

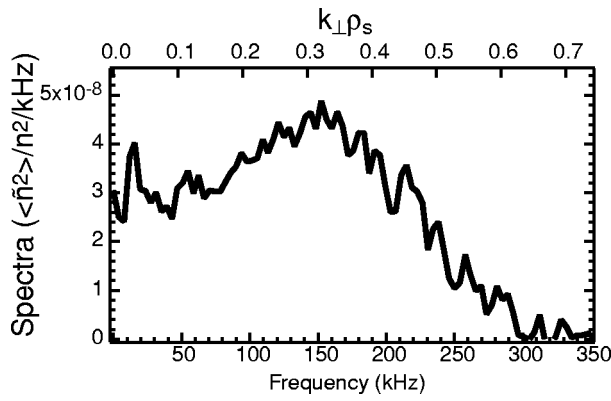


FIG. 5. The measured fluctuation spectrum (amplitude squared) vs frequency and wave number. (Here, $T_e \approx T_i$ and $\rho_s \approx \rho_i$.)

ever, initial gyrokinetic calculations with the Eulerian gyrokinetic GS2 code do not improve the agreement with experiment.³¹ Variation of the plasma gradients across the computation domain might also affect the result. This is the subject of current research, for example, with full-radius particle-simulation codes,^{32,33} or finite-annulus Eulerian gyro-kinetic codes.³⁴ Much further work is required to establish definitively the causal connection between turbulence and transport. We are presenting this case in detail in order to provide a reference and context for subsequent studies.

II. THE EXPERIMENTAL DATA

We deliberately choose a shot that is expected to have substantial turbulence in the outer part of the core. That is, the maximum growth rate without flow shear should substantially exceed the flow-shear frequency. The shot in question, No. 98777, is an L -mode in DIII-D, which is used as a reference for comparison with a radiation-improved discharge obtained by neon puffing.^{8,35} The measured density and temperature profiles are shown in Figs. 1–4 for $t=1150$ –1170 ms into the discharge. The deuterium ion density (not shown) and Z_{eff} are inferred assuming the carbon is six times ionized. (We do not consider the neon-puffed shot 98775 here, because the ITG modes are expected to be stable. This results from a reduction of the driving terms together with increased flow shear and accounts for the improved confinement.)

BES measurements were taken at $t=1100$ –1200 ms at the normalized radius $\rho=0.7$ near the outer plasma mid-plane. After converting relative intensity to relative density and correcting for sample volume effects, we estimate the relative density fluctuation level, to be $|\tilde{n}/n| \leq 0.4\%$. The spectrum as a function of frequency and wavenumber is shown in Fig. 5. Here, $k_{\perp} = k_{\theta}$ is inferred from the dominant $\mathbf{E} \times \mathbf{B}$ Doppler shift, $\omega \approx k_{\theta} v_E$, since the mean frequency in the plasma frame is small. The wave number is normalized to $\rho_s = c_s / \omega_{ci}$, where $c_s = \sqrt{T_e / m_i}$. The peak at $k_{\perp} \rho_s \approx 0.32$ may shift to a somewhat higher value when corrected for sample volume.

Energy and particle fluxes obtained in a power-balance analysis (using the TRANSP code) for the target radius and time are given in Table I. The ion quantities include both the

TABLE I. Experimental transport losses through the surface $\rho=0.7$ at $t=1160$ msec of the reference shot, 98 777. Here, $A=37.5$ m² is the area of the flux surface.

| Particle fluxes | Loss through surface particles/s | Diffusivity m ² /s |
|-----------------------------|--|----------------------------------|
| Ions | $\Gamma_i A = 1.6 \times 10^{21}$ | $D_i = 1.3$ |
| Electrons | $\Gamma_e A = 1.9 \times 10^{21}$ | $D_e = 1.4$ |
| Energy fluxes | Loss through surface MW | Diffusivity m ² /s |
| Ion thermal conduction | $q_i A = 1.3$ | $\chi_i = 3.8$ |
| Ion thermal convection | $\frac{3}{2} \Gamma_i T_i A = 0.2$ | |
| Total ion thermal flux | $Q_i A = q_i A + \frac{3}{2} \Gamma_i T_i A = 1.5$ | $\chi_i^{\text{eff}} = 4.4$ |
| Electron thermal conduction | $q_e A = 1.2$ | $\chi_e = 2.3$ |
| Electron thermal convection | $\frac{3}{2} \Gamma_e T_e A = 0.2$ | |
| Total electron thermal flux | $Q_e A = q_e A + \frac{3}{2} \Gamma_e T_e A = 1.4$ | $\chi_e^{\text{eff}} = 2.8$ |
| Total thermal flux | $(Q_e + Q_i) A = 2.9$ | |

main deuterium and the impurity carbon. We note that in total, i.e., for the full plasma volume, there is about 3.6 MW of electron and ion heating. Of this amount, about 0.5 MW is ohmic, which implies that only 3.1 MW of the total injected 4.5 MW of beam power is absorbed by the plasma. Most of this energy is deposited inside the $\rho=0.7$ surface, transported by the ions and electrons through that surface and then lost by radiation at larger radii.

For comparison with other presentations^{8,35} we also list the corresponding thermal and particle diffusivities implied by a diagonal transport model for the profiles shown, e.g., taking the conducted heat flux to be $q_i = \chi_i n_i T_i / L_{Ti}$, where the scale length $L_{Ti} = (d \ln T_i / dr)^{-1}$ is an average over the flux surface. Similarly, the total energy flux is given by $Q_i = \chi_i^{\text{eff}} n_i T_i / L_{Ti}$. For comparison with theory we prefer to use the fluxes, since their experimental values depend on integrated quantities and not on local gradients. In this framework the diffusivities, e.g., χ_i , are secondary derived quantities. For the radially localized simulations, of course, we must still deal with uncertainties in the input local gradients.

III. THE CODE AND SIMULATION OUTPUT

GRYFFIN or ITG is a nonlinear GLF code that computes turbulence in a flux tube centered at the chosen radius.^{11,12} It makes use of ballooning formalism, taking the sheared magnetic geometry from the EFIT equilibrium. GRYFFIN calculates the evolution of a main ion species and one or more impurity species. The electron response includes a nonadiabatic trapped electron contribution. Thus, transport of both energy and particles is calculated, and trapped electron modes and impurity drift waves are included along with ITG modes. Although an electromagnetic version has been developed^{36,37} the code used here is electrostatic. At $\rho=0.7$ drift-Alfvén coupling is slightly stabilizing, but by an amount far too small to affect the experimental comparison. A principal saturation mechanism arises from the toroidally and poloidally symmetric modes, i.e., the zonal flows. Background $\mathbf{E} \times \mathbf{B}$ flow shear, however, is not included.

We choose a flux-tube size and number of poloidal and radial mode numbers sufficient to encompass the perpendicular correlation lengths and resolve the mode spectrum up to

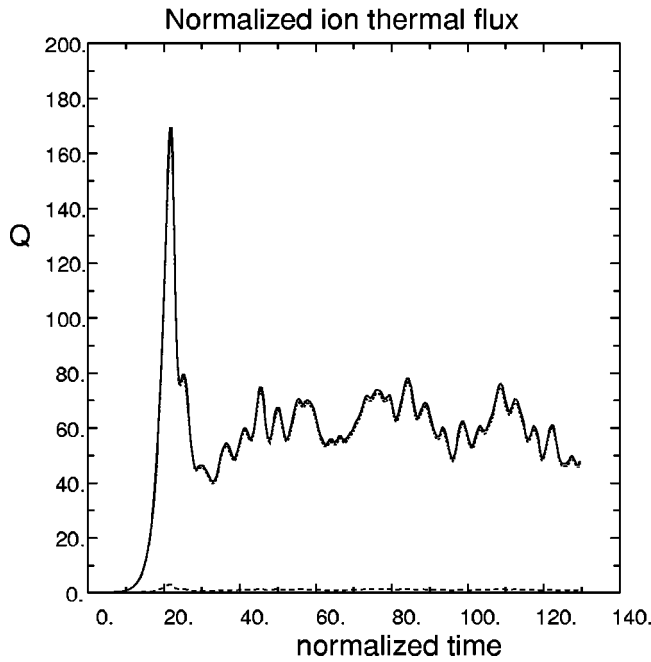


FIG. 6. Normalized total energy transport vs time from the gyrofluid simulation, flux-surface averaged: for the main ions (dotted line) and impurities (dashed line) and their sum (solid line).

$k_{\theta}\rho_i \geq 1.0$. The precise upper bound of k_{θ} depends on the growth-rate spectrum of the ITG and impurity modes. The code is configured to run in parallel on the T3E (MCURIE) at the National Energy Research Scientific Computing Center (NERSC). For our cases the number of processors is set equal to the number of poloidal modes, typically 22, including $k_{\theta}=0$. The run we shall present represents about 16 000 time steps and 3.7 CPU hours on each of the 22 processors.

We work with fixed profiles because it is the only way at present to focus on the turbulence itself. A long-term goal, presently beyond our capability, is to couple the simulations to a transport code. Since the anomalous transport leads to stiff systems of equations, meaning that transport fluxes vary strongly with small profile changes, running a transport simulation is the only way to fully test a transport model derived from turbulence simulations. This is a consequence of the critical-gradient nature of ITG turbulence.²⁹ We could partly overcome this limitation by running the turbulence simulations at several radii. While we do not report on such an exercise here, we offer some further comments in Sec. V.

All input and output quantities are normalized to typical gyrokinetic time and length scales, e.g., time to L_{ne}/v_{Ti} , k_{\parallel} to L_{ne}^{-1} , and k_{\perp} to ρ_i^{-1} . Here the gradient scale length is defined by $L_{ne} = a(dn_e/d\rho)^{-1}$, where a is half the plasma diameter at the midplane, and ρ is the normalized flux-surface label. The thermal velocity and gyroradius are defined by $v_{Ti} = \sqrt{T_i/m_i}$ and $\rho_i = v_{Ti}/\omega_{ci}$, respectively. A typical time plot is shown in Fig. 6. Here, we show the total thermal fluxes, Q_i , of the deuterium and carbon ions and their sum, normalized to $n_e T_i \rho_i^2 v_{Ti} / L_{ne}^2$, as functions of $t v_{Ti} / L_{ne}$. In this example, the impurity concentration is low, and the turbulence is dominated by ordinary ITG modes, whose growth rate is enhanced by the trapped electrons. The

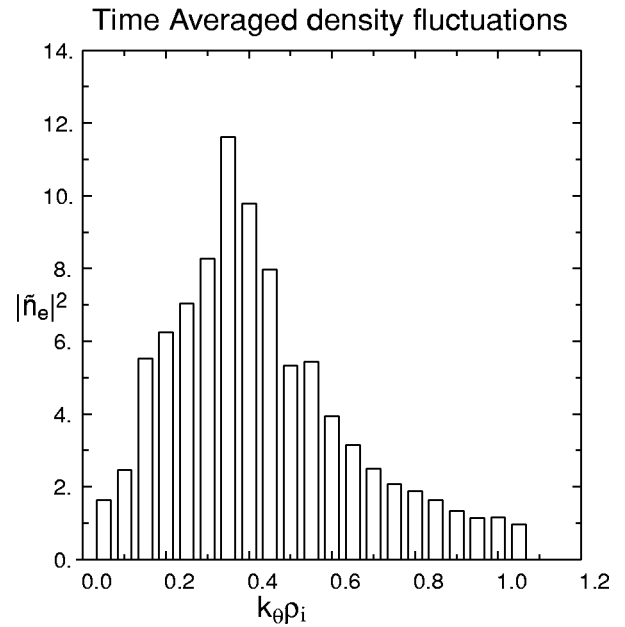


FIG. 7. Relative density fluctuation spectrum vs $k_{\theta}\rho_i$ normalized to ρ_i^2/L_n^2 .

contribution of the impurity ions to the transport is quite small, nearly invisible on the plot. Plots similar to Fig. 6 are also obtained for the electron thermal flux and the particle fluxes. The latter arise from the nonadiabatic effect of the trapped electrons. Averaged in the same way, the spectrum of the squared relative density fluctuations, normalized to ρ_i^2/L_{ne}^2 , is shown in Fig. 7 as a function of $k_{\theta}\rho_i$. Many other diagnostic quantities are available in the code output.

IV. COMPARISON OF SIMULATION RESULTS WITH DATA

To compare with the measurements, we first note that the simulated wavenumber spectrum of Fig. 7 is very similar in shape to the BES spectrum of Fig. 5, each having a peak in the neighborhood of $k_{\theta}\rho_s \approx k_{\theta}\rho_i \approx 0.32-0.35$. (The electron and ion temperatures are nearly equal at this radius.) Summing over the simulated spectrum and converting from the normalized units, however, we find $|\tilde{n}_e/n_e| \approx 2.0\%$, which is substantially larger than the BES value. This is without any flow-shear correction.

We define the particle and thermal losses to be the time averages over the final 3/4 of the time series plotted in Fig. 6 and the corresponding time series for the other fluxes, i.e., after the initial transient. Converting to dimensional units, we find, for example, that the uncorrected ion energy loss by thermal conduction is $Q_i A = 3.5 \pm 0.2$ MW, where the error quoted is the standard deviation of the averaged time series. This exceeds the experimental value given in Table I by a factor of 2.3. (We ignore neoclassical transport, which accounts for about 10% of ion thermal flux.)

There is considerable evidence that the background flow shear strongly affects the turbulence levels and transport. This strong effect for the neon-puffed case relative to our reference case has been shown in a global simulation with adiabatic electrons.⁸ However, quantitative comparisons with

TABLE II. Comparison of experimental and simulated particle and energy transport losses and relative density fluctuations. To account for the flow-shear effect the simulated quantities in column 3 are corrected by the factor $(1 - \omega_E / \gamma_{\max}) = 0.65$ and 0.86 , respectively, the smaller figure being that of the Hahm–Burrell form and the larger being that of the Waltz–Miller form. The last column gives the differences between the experimental values and the simulation.

| | Experimental | Simulation, corrected for | Difference: |
|-----------------------------|----------------------|------------------------------|---------------------------|
| Particle losses | (particles/s) | ω_E (particles/s) | ETG? (particles/s) |
| $\Gamma_i A$ | 1.6×10^{21} | $2.3, 3.1 \times 10^{20}$ | $1.4, 1.3 \times 10^{21}$ |
| $\Gamma_e A$ | 1.9×10^{21} | $4.7, 6.2 \times 10^{20}$ | $1.4, 1.3 \times 10^{21}$ |
| Energy losses | (MW) | (MW) | (MW) |
| $q_i A$ | 1.3 | 2.2, 3.0 | -0.9, -1.7 |
| $Q_i A$ | 1.5 | 2.2, 3.0 | -0.7, -1.5 |
| $q_e A$ | 1.2 | 0.7, 1.0 | 0.5, 0.2 |
| $Q_e A$ | 1.4 | 0.8, 1.1 | 0.6, 0.3 |
| Fluctuations | | | |
| $ \tilde{n}_e / n_e $ | 0.4% | 1.6%, 1.9% | |
| $k_{\theta} \rho_i$ of peak | 0.32 | 0.35 | |

the experiment were not made. Waltz *et al.*²⁵ have studied this question by means of numerical simulation and inferred that the transport levels without sheared flow should be corrected by the factor $(1 - \omega_E / \gamma_{\max})$, where ω_E is the shearing frequency and γ_{\max} is the maximum linear growth rate of the modes. This is known as the “quench rule.” For our case, these quantities are $\omega_E = 2.5 \times 10^4 \text{ s}^{-1}$ and $\gamma_{\max} = 7 \times 10^4 \text{ s}^{-1}$, where we use the definition of ω_E given by Hahm and Burrell.³⁸ Waltz and Miller³⁹ propose an alternative formula for ω_E , which in its simplest approximation is $\omega_E \approx (r/q)d(qv_E/r)/dr$ and in general is a flux function. For shaped discharges, it is smaller than the Hahm–Burrell evaluation and for our case is given by $\omega_E = 9.7 \times 10^3 \text{ s}^{-1}$. The maximum growth rate given by the GRYFFIN code agrees with that found with an electromagnetic gyrokinetic code.⁸ Thus, we have $(1 - \omega_E / \gamma_{\max}) = 0.65$ or 0.86 , depending on which evaluation of the flow shear we accept. We note also that recent gyrokinetic simulations by Dimits⁴⁰ indicate that the required flow shear for stabilization may be as much as four times that of the preceding formula. We give a range of comparisons in Table II.

The transport fluxes and turbulence amplitudes, converted to dimensional units and with the flow-shear factor applied, are compared with the experimental values in columns 2 and 3 of Table II. Applying the flow-shear factor to the square of the fluctuation amplitude, we find our density fluctuation estimate is $|\tilde{n}_e / n_e| \approx 1.6\text{--}1.9\%$, which is still large compared with the measurement by a factor of 4 or more. (Neither the simulation nor the experimental estimate includes high wave-number modes such as ETG.) The peak at $k_{\theta} \rho_i \approx 0.35$ in the simulation has not been corrected for flow shear and is likely to shift to a higher value when flow shear is applied in the simulation runs.²⁵ Thus, it may track the sample-volume-corrected measured spectrum.

We see that, with the flow-shear correction, the simulation yields an ion thermal conduction value that is larger than the measurement. On the other hand, it gives particle and

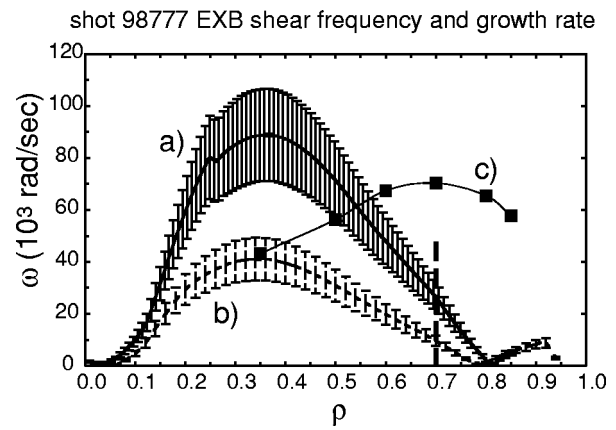


FIG. 8. Both forms of shear flow frequency and ITG growth rate for the reference shot vs the normalized radius: (a) using the Hahm–Burrell formula, and (b) using the Waltz–Miller formula, and (c) ITG growth rate. The errors are small in the neighborhood of $\rho = 0.7$ (vertical dashed line), where the BES measurements are made.

convection fluxes of both species that are negligible compared to the TRANSP analysis. The simulated electron thermal flux is small by approximately a factor of 2. Again, note that the particle and electron thermal transport in the code come entirely from the trapped electron dissipation. (We will return to column 4 of Table II in the next section.)

V. DISCUSSION AND CONCLUSIONS

The ITG modes with impurity and trapped electron effects, as simulated by the GRYFFIN code, are clearly more than sufficient to account for the thermal transport of the ions observed in the experiment at the radius chosen, and the fluctuation levels are overestimated by a large factor. On the other hand, electron thermal and particle transport are not accounted for by the simulated ITG modes. We therefore consider some of the uncertainties and additional physical effects that might bring the turbulence calculations into conformity with the experiments. We also consider whether the case we have chosen is representative or is unusual in some way.

$E \times B$ shearing and zonal flows. Both forms of the flow-shear frequency and the maximum ITG growth rate are shown as functions of radius in Fig. 8. First, the shearing rate itself is uncertain by about 20%, but at $\rho = 0.7$ the uncertainty is a small fraction of the quench-rule correction, since the discharge is well above marginal.

Second, there is considerable uncertainty in the quench rule itself. Some of the curves in Ref. 25 show a concave rather than linear dependence of the transport on ω_E . On the other hand, Hamaguchi and Horton, in a fluid slab model, obtain a convex dependence on ω_E ,⁴¹ as does Dimits,⁴⁰ who also finds a weaker dependence on ω_E . Also, as noted earlier, the Waltz and Miller³⁹ form of ω_E is a flux function that can be smaller than that of Hahm and Burrell³⁸ by as much as a factor of 2.5. The point where the growth rate and the flow-shear rate cross is often identified with an internal transport barrier. Judging by the profiles of Figs. 3 and 4, however, such a barrier appears to be nonexistent, in the reference discharge, indicating that one should use caution in

applying this criterion. A case could be made for marginal stability around $\rho=0.4$, providing support for the Waltz–Miller flow-shear frequency, but this highlights the difficulty of explaining why the transport is not stronger near $\rho\approx 0.7$.

Third, the treatment of radial modes or zonal flows continues to be a subject of some controversy, with GLF codes yielding lower zonal flows and higher turbulent transport than the gyrokinetic codes.²⁹ It is possible that an improved treatment of zonal flows⁴² in GRYFFIN could improve the agreement. We are also investigating this hypothesis with the GS2 gyrokinetic code.^{21,22,44} We have so far found that these effects are insufficient to explain the discrepancy between the simulation and the data for the reference case and other similar cases in DIII-D and Alcator C-Mod.^{30,31} Finally, there is the possibility that the effects of flow shear could alter the wave-number spectrum in a way that affects our interpretation of the BES measurement. In particular, initial tests with flow shear included in GRYFFIN⁴² suggest greatly broadened radial wave-number spectra. These might be filtered by the finite sample volume, yielding a lower experimental value than is reported in the simulation. As noted earlier, these calculations present some difficulties and are not yet ready for presentation.

Profile uncertainties. We have shown in separate work²⁸ that uncertainties in the local input gradients can have a strong effect on the simulation results. In particular, in plasmas with $Z_{\text{eff}} > 2$ variations in the impurity density gradient within the estimated error bars can change the fluxes substantially. This comes about mainly through the dilution effect. That is, the background ion density gradient (not measured independently) must change to maintain charge neutrality. This change in the main ion gradient with neon puffing is likely to be the initiating event that leads to improved confinement.^{7,43} In the reference case considered here, however, $Z_{\text{eff}} \approx 1.5$, and the impurity effect is small. Our experience with these studies indicates that the transport fluxes and the fluctuation levels tend to vary in proportion to one another as the profile gradients are varied. Thus, by this approach we cannot expect much relief from the seeming inconsistency of turbulence levels relative to the transport.

The discrepancy with the experimental ion thermal transport might be accounted for by the uncertainty in the temperature gradient. Figure 4 illustrates the scatter in the data points. If, at this time and radius, the temperature profile is flatter than we have assumed, then reducing our input gradient might be helpful. Figure 9 shows the ion energy flux, both with and without the flow-shear corrections as a function of ion temperature gradient. With the Hahn–Burrell flow shear, we see that reducing the temperature gradient by 20%, from $R/L_{Ti} = 8.7$ to 7.2 achieves agreement. One must be cautious, however, in accepting this as an explanation because of the preceding discussion of flow shear and because the simulated fluctuation levels remain too high. To correct both the fluctuation levels and the transport fluxes, we would require first a fourfold decrease in \tilde{n}_e/n_e and then an adjustment of the phase between the fluctuating temperature and electric field that actually enhances the fluxes.

We also note that flattening the profile at one radius re-

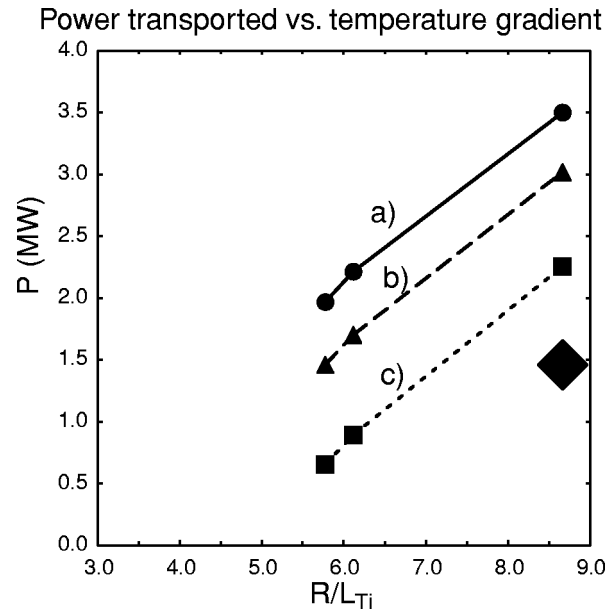


FIG. 9. Total energy flux through surface at $\rho=0.7$ vs temperature gradient, showing the experimental value (large diamond) and simulated values (a) with no $\mathbf{E} \times \mathbf{B}$ correction, and with the shear flow correction using (b) the Waltz–Miller formula and (c) the Hahn–Burrell formula.

quires raising it somewhere else to maintain global consistency. Because the experimental transport fluxes and the code input parameters vary slowly with radius, the problem will reappear at some other radius. Finally, we note in Fig. 7 that the flow-shear parameter passes through zero near $\rho = 0.8$ but no great differences in the transport are seen there. We have found similar results for an H mode in Alcator C-Mod. We conclude that, as far as GRYFFIN simulations are concerned, the results presented here are representative of the outer radii of both L and H modes.

ETG modes. We might adjust the profiles, e.g., increasing the electron temperature gradient to fit the electron thermal transport, but the preceding discussion applies here as well. We may also assume that other effects, such as electron temperature-gradient (ETG) modes can account for some of it. There is evidence from theory and computer simulations that ETG modes play a role in anomalous transport.^{21,22} A plausible speculation is given in Table II. Column 4 lists the difference between the measured values, column 2, and those of our simulation, column 3. ETG modes could account for the difference in the electron thermal transport. Until an ETG simulation is run for this particular case we cannot directly test this idea. To the extent that the ions are approximately adiabatic, ETG modes are not expected to drive much particle transport. Trapped electron modes with wave numbers between the ITG and the ETG ranges could play a role in both particle and electron thermal transport.

Profile variations or ρ^* dependence. The present calculations are performed in a flux tube with fixed plasma gradients. Thus, profile variations or finite ρ^* effects, where ρ^* is the ratio of the gyroradius to a macroscopic length, cannot be addressed here. That is, by definition the results exhibit gyro-Bohm scaling. Studies with full-radius gyro-kinetic particle codes,^{32,33} and with a finite-annulus Eulerian gyrokinetic

code³⁴ have shown departures from gyro-Bohm in the direction of Bohm scaling. Reductions in transport fluxes with respect to the flux-tube results have been found.⁴⁵ Whether these would be sufficient to bring our results into conformity with the measurements is not known.

In summary, we have an encouraging start in the direct comparison of turbulence simulations to experimental measurements, in which both the fluctuations and transport are taken into consideration. The simulated ion thermal transport level exceeds that of the experiment. It could be brought into agreement within the error bars of the temperature gradient and flow shear, but we argue that some unaccounted for stabilizing mechanism should be sought. The most significant remaining problems are (1) the turbulence levels predicted remain a few times larger than the BES measurements, and (2) we have no explanation for the measured particle flux. These results provide a further strong incentive to seek an explanation.

We expect that by a combination of theoretical improvements and experimental refinement the gaps between the simulations and measurements will continue to be reduced. Future work with GRYFFIN will be to complete the calculations with the background flow shear and improved zonal flow treatment. We will also continue nonlinear gyrokinetic runs with the nonlinear GS2 code.^{21,22,44}

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¹W. Horton, Rev. Mod. Phys. **71**, 735 (1999).

²B. A. Carreras, IEEE Trans. Plasma Sci. **25**, 1281 (1997).

³D. L. Brower, M. H. Redi, W. M. Tang, R. V. Bravenec, R. D. Durst, S. P. Fan, Y. X. He, S. K. Kim, N. C. Luhmann, Jr., S. C. McCool, A. G. Meigs, M. Nagatsuo, A. Ouroua, W. A. Peebles, P. E. Phillips, T. L. Rhodes, B. Richards, C. P. Ritz, W. L. Rowan, and A. J. Wootton, Nucl. Fusion **29**, 1247 (1989).

⁴R. V. Bravenec, K. W. Gentle, B. Richards, D. W. Ross, D. C. Sing, A. J. Wootton, D. L. Brower, N. C. Luhmann, Jr., W. A. Peebles, C. X. Yu, T. P. Crowley, J. W. Heard, R. L. Hickok, P. M. Schoch, and X. Z. Yang, Phys. Fluids B **4**, 2127 (1992).

⁵R. J. Fonck, N. Bretz, G. Cosby, R. Durst, E. Mazzucato, R. Nazikian, S. Paul, S. Scott, W. Tang, and M. Zarnstorff, Plasma Phys. Controlled Fusion **34**, 1903 (1992).

⁶R. J. Fonck, G. Cosby, R. D. Durst, S. F. Paul, N. Bretz, S. Scott, E. Synakowski, and G. Taylor, Phys. Rev. Lett. **70**, 3736 (1993).

⁷G. R. McKee, K. H. Burrell, R. J. Fonck, G. L. Jackson, M. Murakami, G. M. Staebler, D. M. Thomas, and W. P. West, Phys. Rev. Lett. **84**, 1922 (2000).

⁸G. R. McKee, M. Murakami, J. A. Boedo, N. H. Brooks, K. H. Burrell, D. Ernst, R. J. Fonck, G. L. Jackson, M. Jakubowski, R. J. LaHaye, A. M. Messiaen, J. Ongena, C. L. Rettig, B. Rice, C. Rost, G. M. Staebler, R. Sydora, D. M. Thomas, B. Unterberg, M. R. Wade, and W. P. West, Phys. Plasmas **7**, 1870 (2000).

⁹K. H. Burrell, Phys. Plasmas **4**, 1499 (1997).

¹⁰E. J. Synakowski, Plasma Phys. Controlled Fusion **40**, 581 (1998).

¹¹W. Dorland and G. W. Hammett, Phys. Fluids B **5**, 812 (1993).

¹²M. A. Beer and G. W. Hammett, Phys. Plasmas **3**, 4046 (1996).

¹³J. L. Luxon and L. G. Davis, Fusion Technol. **8**, 441 (1985).

¹⁴K. W. Gentle, R. V. Bravenec, G. Cima, G. A. Hallock, P. E. Phillips, D. W. Ross, W. L. Rowan, and A. J. Wootton, Phys. Plasmas **4**, 3599 (1997).

¹⁵W. M. Kissick, E. D. Frederickson, J. D. Callen, C. E. Bush, Z. Chang, P. C. Efthimion, R. A. Hulse, D. K. Mansfield, H. K. Park, J. F. Schivell, S. D. Scott, E. J. Synakowski, G. Taylor, and M. C. Zarnstorff, Nucl. Fusion **34**, 349 (1994).

¹⁶V. V. Parail, A. Cherubini, J. G. Cordey, M. Erba, P. Galli, R. Giannella, L. Porte, F. Romanelli, A. Rookes, E. M. Springman, and A. Taroni, Nucl. Fusion **37**, 481 (1997).

¹⁷P. Mantica, P. Galli, G. Gorini, G. M. D. Hogeweij, J. de Kloe, N. J. Lopes Cardozo, and RTP Team, Phys. Rev. Lett. **82**, 5048 (1999).

¹⁸G. McKee, R. Ashley, R. Durst, R. Fonck, M. Jakubowski, K. Tritz, K. Burrell, C. Greenfield, and J. Robinson, Rev. Sci. Instrum. **70**, 913 (1999).

¹⁹G. McKee, R. Ashley, R. Durst, R. Fonck, M. Jakubowski, K. Tritz, K. Burrell, C. Greenfield, and J. Robinson, Rev. Sci. Instrum. **70**, 2179 (1999).

²⁰R. J. Fonck, P. A. Duperrex, and S. F. Paul, Rev. Sci. Instrum. **61**, 3487 (1990).

²¹F. Jenko, W. Dorland, M. Kotschenreuther, and B. N. Rogers, Phys. Plasmas **7**, 1904 (2000).

²²W. Dorland, F. Jenko, M. Kotschenreuther, and B. N. Rogers, Phys. Rev. Lett. **85**, 5579 (2000).

²³R. J. Hawryluk, in *Physics of Plasmas Close to Thermonuclear Conditions*, edited by B. Coppi, G. G. Leotta, D. Pfirsch, R. Pozzoli, and E. Sindoni (Pergamon, Oxford, 1980), Vol. 1, p. 19.

²⁴L. L. Lao, H. St. John, R. D. Stambaugh, A. G. Kellman, and W. Pfeiffer, Nucl. Fusion **25**, 1611 (1985).

²⁵R. E. Waltz, R. L. Dewar, and X. Garbet, Phys. Plasmas **5**, 1784 (1998).

²⁶D. W. Ross, R. V. Bravenec, C. P. Ritz, M. L. Sloan, J. R. Thompson, A. J. Wootton, P. M. Schoch, J. W. Heard, T. P. Crowley, R. L. Hickok, V. Simicic, D. L. Brower, W. A. Peebles, and N. C. Luhmann, Jr., Phys. Fluids B **3**, 2251 (1991).

²⁷R. V. Bravenec and A. J. Wootton, Rev. Sci. Instrum. **66**, 802 (1995).

²⁸D. W. Ross, R. V. Bravenec, W. Dorland, M. A. Beer, and G. W. Hammett, Bull. Am. Phys. Soc. **44**, 213 (1999).

²⁹A. M. Dimits, G. Bateman, M. A. Beer, B. I. Cohen, W. Dorland, G. W. Hammett, C. Kim, J. E. Kinsey, M. Kotschenreuther, A. H. Kritiz, L. L. Lao, J. Mandrekas, W. M. Nevins, S. E. Parker, A. J. Redd, D. E. Shumaker, R. Sydora, and J. Weiland, Phys. Plasmas **7**, 969 (2000).

³⁰W. Dorland, B. N. Rogers, F. Jenko, M. Kotschenreuther, G. W. Hammett, D. Mikkelsen, D. W. Ross, M. A. Beer, P. B. Snyder, R. Bravenec, M. Greenwald, D. Ernst, and R. Budny, in *Fusion Energy 2000* (International Atomic Energy Agency, Vienna, 2001). (Paper TH2/5, published as CD-ROM. Also see <http://www.iaea.org/programmes/ripc/physics/fec2000/html/fec2000.htm>.)

³¹D. W. Ross, R. V. Bravenec, W. Dorland, M. A. Beer, G. W. Hammett, G. R. McKee, M. Murakami, and G. L. Jackson, Bull. Am. Phys. Soc. **45**, 150 (2000).

³²R. D. Sydora, V. K. Decyk, and J. M. Dawson, Plasma Phys. Controlled Fusion **38**, A281 (1996).

³³Z. Lin, T. S. Hahm, W. W. Lee, W. M. Tang, and R. B. White, Phys. Plasmas **7**, 1857 (2000).

³⁴J. Candy, R. E. Waltz, and M. N. Rosenbluth, in *Proceedings of the 28th European Conference on Controlled Fusion and Plasma Physics*, Madeira, Portugal (The European Physical Society, to be published).

³⁵M. Murakami, G. R. McKee, G. L. Jackson, G. M. Staebler, D. R. Baker, J. A. Boedo, N. H. Brooks, K. H. Burrell, E. Ernst, T. E. Evans, J. E. Kinsey, R. J. LaHaye, L. L. Lao, A. M. Messiaen, J. Ongena, C. L. Rettig, G. Rewoldt, H. E. S. John, D. M. Thomas, M. R. Wade, and W. P. West, Bull. Am. Phys. Soc. **44**, 127 (1999).

³⁶P. B. Snyder, Ph.D. dissertation, Princeton University, 1999.

³⁷P. B. Snyder, G. W. Hammett, M. A. Beer, and W. Dorland, in *Proceedings of the 26th European Conference on Controlled Fusion and Plasma Physics, Maastricht, 1999* (The European Physical Society, 1999), Vol. 23J, p. 1685.

- ³⁸T. S. Hahm and K. H. Burrell, Phys. Plasmas **2**, 1648 (1995).
³⁹R. E. Waltz and R. L. Miller, Phys. Plasmas **6**, 4265 (1999).
⁴⁰A. Dimits (private communication).
⁴¹S. Hamaguchi and W. Horton, Phys. Fluids B **4**, 319 (1992).
⁴²M. A. Beer and G. W. Hammett, Bull. Am. Phys. Soc. **44**, 300 (1999).
⁴³M. Z. Tokar, J. Ongena, B. Unterberg, and R. R. Weynants, Phys. Rev. Lett. **84**, 895 (2000).
⁴⁴M. Kotschenreuther, G. Rewoldt, and W. M. Tang, Comput. Phys. Commun. **88**, 128 (1995).
⁴⁵R. E. Waltz (private communication).